

Finite series

- ▶ $\sum_{n=1}^N n = \frac{N(N+1)}{2}$
- ▶ $\sum_{n=1}^N n^2 = \frac{N(N+1)(2N+1)}{6}$
- ▶ $\sum_{n=1}^N n^3 = \frac{N^2(N+1)^2}{4}$
- ▶ $\sum_{n=0}^N x^n = \frac{x^{N+1} - 1}{x - 1}$
- ▶ $\sum_{n=0}^N \frac{N!}{n!(N-n)!} x^n y^{N-n} = (x+y)^N$
- ▶ $\sum_{n=0}^N e^{j(\theta + n\phi)} = \frac{\sin[(N+1)\phi/2]}{\sin(\phi/2)} e^{j[\theta + (N\phi/2)]}$
- ▶ $\sum_{n=0}^N \binom{N}{n} = \sum_{n=0}^N \frac{N!}{n!(N-n)!} = 2^N$

Infinite series

- ▶ $e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots = \sum_{n=0}^{\infty} \frac{x^n}{n!}$

Error Function

- ▶ $\text{erf}(x) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^x e^{-y^2/2} dy$
- ▶ $\text{erfc}(x) = \frac{1}{\sqrt{2\pi}} \int_x^{\infty} e^{-y^2/2} dy$
- ▶ $\text{erfc}(x) \simeq \frac{1}{x\sqrt{2\pi}} \left(1 - \frac{1}{x^2}\right) e^{-x^2/2}$
- ▶ $\text{erf}(x) + \text{erfc}(x) = 1$