

Basic Forms
▶ $\int u \, dv = \, vu \, - \int v \, du$ ▶ $\int x^n \, dx = \frac{1}{n+1} x^{n+1} + C \, (n \neq -1)$ ▶ $\int \frac{1}{x} \, dx = \ln x + C$ ▶ $\int e^x \, dx = \, e^x + C$ ▶ $\int a^x \, dx = \frac{1}{\ln a} a^x + C$ ▶ $\int \sin x \, dx = - \cos x + C$ ▶ $\int \cos x \, dx = \sin x + C$ ▶ $\int \sec^2 x \, dx = \tan x + C$ ▶ $\int \csc^2 x \, dx = - \cot x + C$ ▶ $\int \sec x \tan x \, dx = \sec x + C$ ▶ $\int \csc x \cot x \, dx = - \csc x + C$ ▶ $\int \tan x \, dx = \ln \sec x + C$ ▶ $\int \cot x \, dx = \ln \sin x + C$ ▶ $\int \sec x \, dx = \ln \sec x + \tan x + C$ ▶ $\int \csc x \, dx = \ln \csc x - \cot x + C$ ▶ $\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C$ ▶ $\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$ ▶ $\int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \sec^{-1} \frac{x}{a} + C$ ▶ $\int \frac{dx}{a^2 - x^2} = \frac{1}{2a} \ln \left \frac{x+a}{x-a} \right + C$ ▶ $\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left \frac{x-a}{x+a} \right + C$

Forms Involving $\sqrt{a^2 + x^2}$, $a > 0$
▶ $\int \sqrt{a^2 + x^2} \, dx = \frac{x}{2} \sqrt{a^2 + x^2} + \frac{a^2}{2} \ln(x + \sqrt{a^2 + x^2}) + C$ ▶ $\int x^2 \sqrt{a^2 + x^2} \, dx = \frac{x}{8} (a^2 + 2x^2) \sqrt{a^2 + x^2} - \frac{a^4}{8} \ln(x + \sqrt{a^2 + x^2}) + C$ ▶ $\int \frac{\sqrt{a^2 + x^2}}{x} \, dx = \sqrt{a^2 + x^2} - a \ln \left \frac{a + \sqrt{a^2 + x^2}}{x} \right + C$ ▶ $\int \frac{\sqrt{a^2 + x^2}}{x^2} \, dx = - \frac{\sqrt{a^2 + x^2}}{x} + \ln(x + \sqrt{a^2 + x^2}) + C$ ▶ $\int \frac{dx}{\sqrt{a^2 + x^2}} = \ln(x + \sqrt{a^2 + x^2}) + C$ ▶ $\int \frac{x^2}{\sqrt{a^2 + x^2}} \, dx = \frac{x}{2} \sqrt{a^2 + x^2} - \frac{a^2}{2} \ln(x + \sqrt{a^2 + x^2}) + C$ ▶ $\int \frac{dx}{x\sqrt{a^2 + x^2}} = - \frac{1}{a} \ln \left \frac{\sqrt{a^2 + x^2} + a}{x} \right + C$ ▶ $\int \frac{dx}{x^2 \sqrt{a^2 + x^2}} = - \frac{\sqrt{a^2 + x^2}}{a^2 x} + C$ ▶ $\int \frac{dx}{(a^2 + x^2)^{3/2}} = \frac{x}{a^2 \sqrt{a^2 + x^2}} + C$
Forms Involving $\sqrt{a^2 - x^2}$, $a > 0$
▶ $\int \sqrt{a^2 - x^2} \, dx = \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \sin^{-1} \frac{x}{a} + C$ ▶ $\int x^2 \sqrt{a^2 - x^2} \, dx = \frac{x}{8} (2x^2 - a^2) \sqrt{a^2 - x^2} + \frac{a^4}{8} \sin^{-1} \frac{x}{a} + C$ ▶ $\int \frac{\sqrt{a^2 - x^2}}{x} \, dx = \sqrt{a^2 - x^2} - a \ln \left \frac{a + \sqrt{a^2 - x^2}}{x} \right + C$ ▶ $\int \frac{\sqrt{a^2 - x^2}}{x^2} \, dx = - \frac{1}{x} \sqrt{a^2 - x^2} - \sin^{-1} \frac{x}{a} + C$ ▶ $\int \frac{x^2 dx}{\sqrt{a^2 - x^2}} = - \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \sin^{-1} \frac{x}{a} + C$ ▶ $\int \frac{dx}{x\sqrt{a^2 - x^2}} = - \frac{1}{a} \ln \left \frac{a + \sqrt{a^2 - x^2}}{x} \right + C$ ▶ $\int \frac{dx}{x^2 \sqrt{a^2 - x^2}} = - \frac{1}{a^2 x} \sqrt{a^2 - x^2} + C$ ▶ $\int (a^2 - x^2)^{3/2} dx = - \frac{x}{8} (2x^2 - 5a^2) \sqrt{a^2 - x^2} + \frac{3a^4}{8} \sin^{-1} \frac{x}{a} + C$ ▶ $\int \frac{dx}{(a^2 - x^2)^{3/2}} = \frac{x}{a^2 \sqrt{a^2 - x^2}} + C$

