

FUNdaMENTALS of Design

Topic 9

Structural Connections & Interfaces



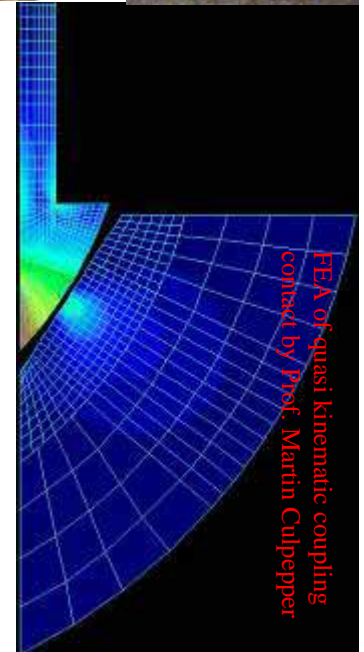
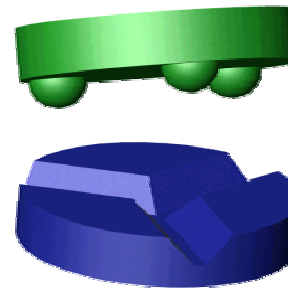
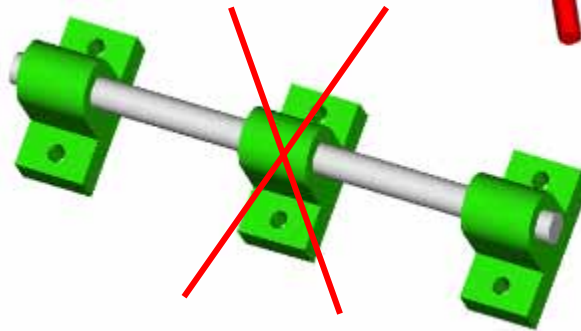
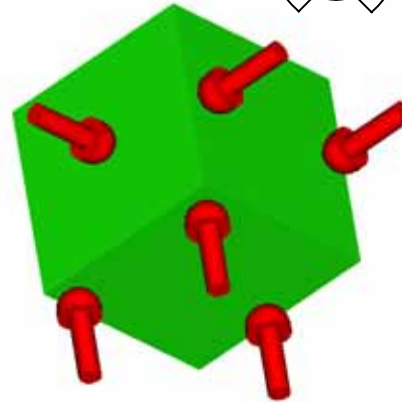
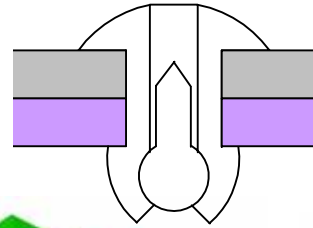
Topic 9

Structural Connections & Interfaces



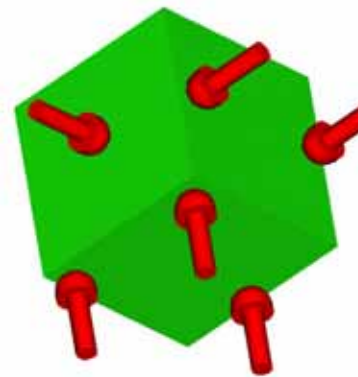
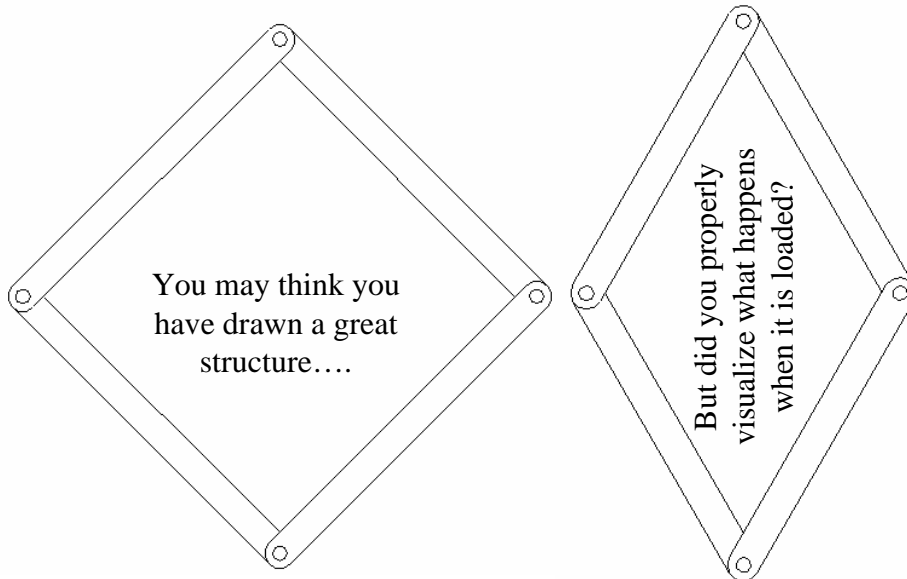
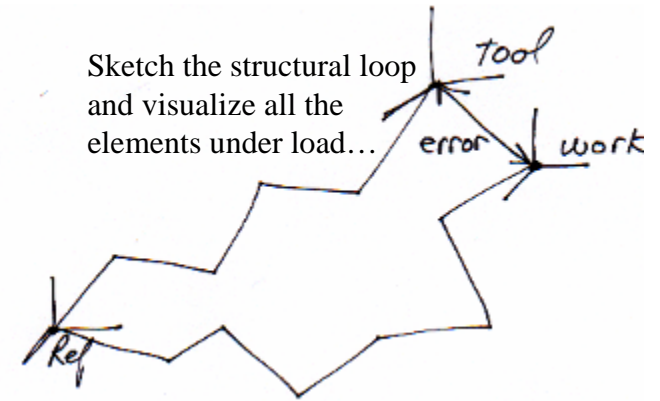
Topics

- Connections
- Structural Joints
- Structural Interfaces
- Hertz Contact
- Kinematic Couplings
- Elastic Averaging

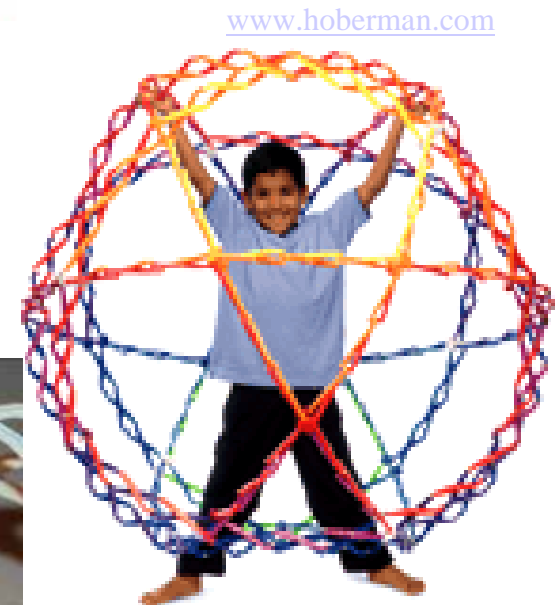


Connections: *Visualization*

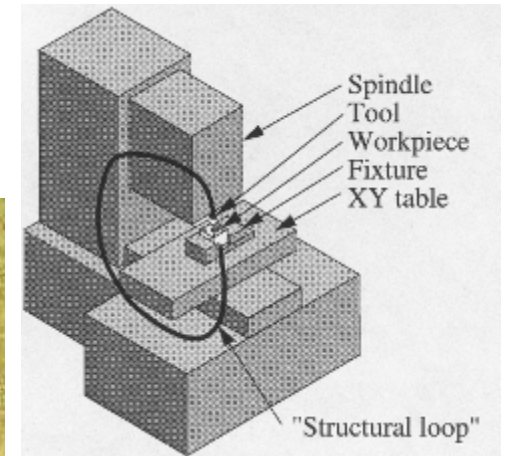
- As a visualization tool for a joint of which are unsure:
 - Make a cardboard model of the joint
 - If the model is stable, there is a good chance that the real parts will also be stable!
- What happens to the performance of your structure if you assume the joints are just pinned?



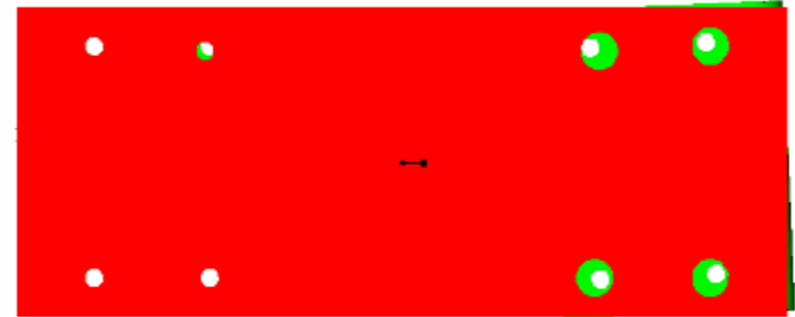
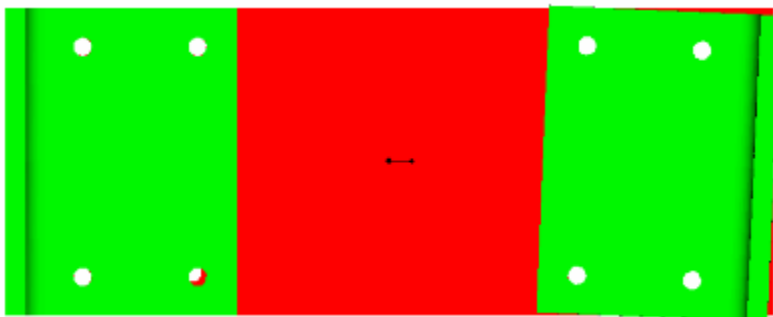
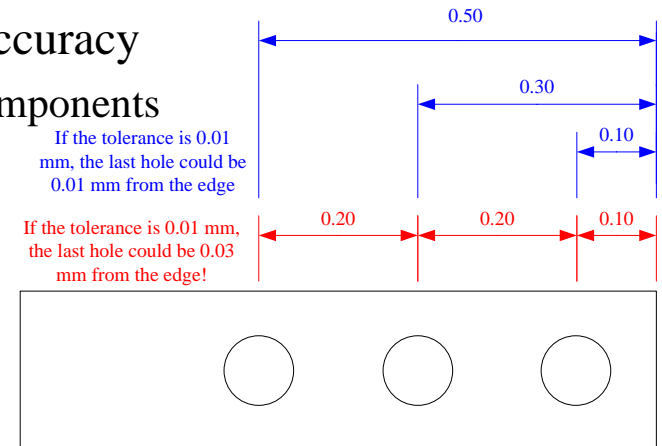
9-2



Connections: *Accuracy*



- Interfaces must enable parts to fit together with the desired accuracy
 - You cannot create two sets of exactly matching holes in two components
 - You can oversize the holes
 - The clearance between the bolts and holes means that the components do not have a unique assembly position
- “Error budgets” keep track of interferences & misalignments
 - These methods often assume “worst case tolerance”
 - For complex assemblies, advanced statistical methods are required
 - Deterministic designs are created using *financial*, *time*, and *error* budgets

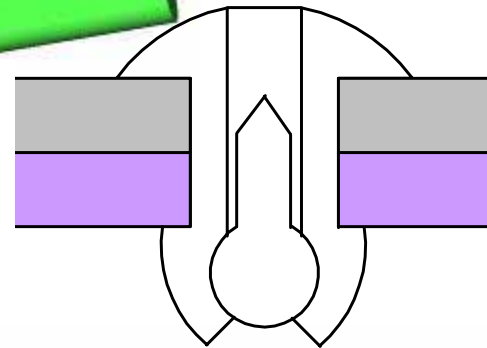
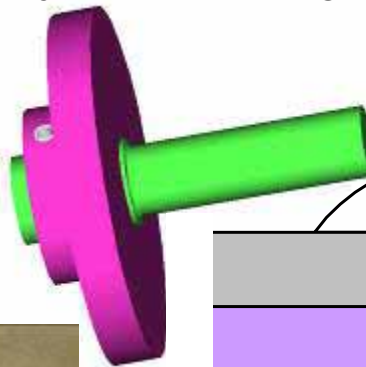
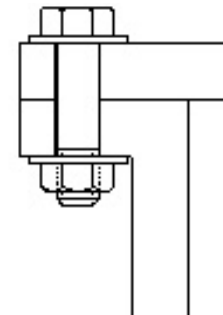




Structural Joints

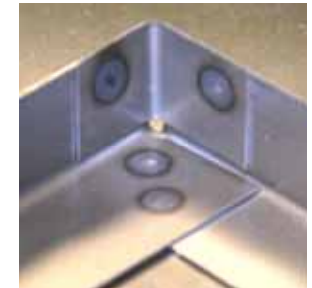
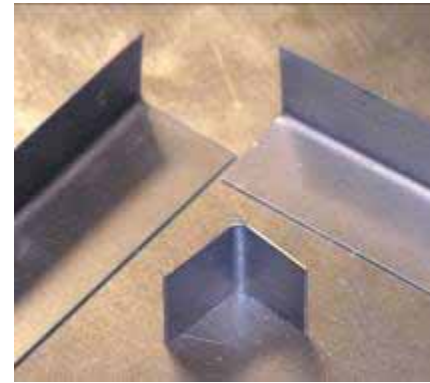


- *Structural joints* (non moving) transfer loads between members, and are a necessary part of almost all structures
 - They can take up space and add cost
 - They can provide damping and design flexibility
- There are many different types of joints including:
 - Welded
 - Adhesive
 - Bolted
 - Pinned & Riveted
 - Press-fit (see page 5-25)

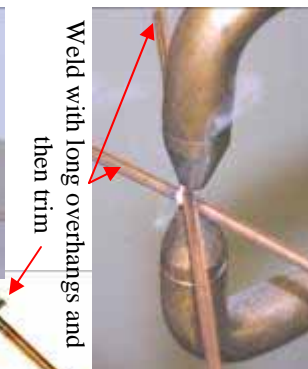
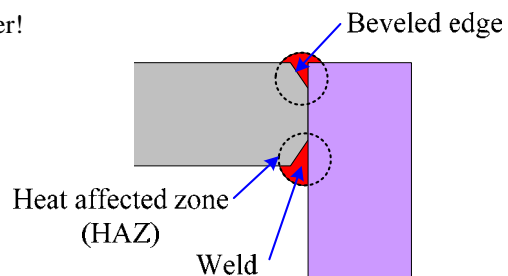


Structural Joints: *Welded*

- A good weld is as strong as the base metal
 - Surface preparation is VERY IMPORTANT
 - Cleanliness
 - On thicker parts, bevel edges to be welded
- Shop personnel will help you with your welding needs
 - Consult with them during the **concept** stage about options
 - Spot welding is used for sheet metal and thin rods
 - Arc welding is typically used for heavier sections
 - TIG (*Tungsten Inert Gas*) is used for welding aluminum, or for very precise welds on steels and special alloys



Steve Haberek, master welder!



Butt Joint: OK



Lap Joint: Good



Tapered Lap Joint: Very Good



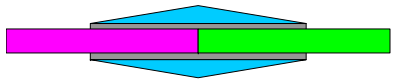
Stepped Lap Joint: Very Good



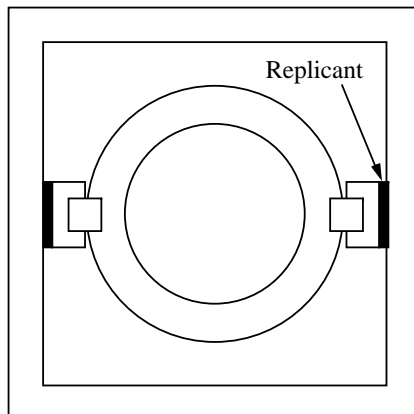
Double Strap Joint: Very Good



Tapered Double Strap Joint: Excellent



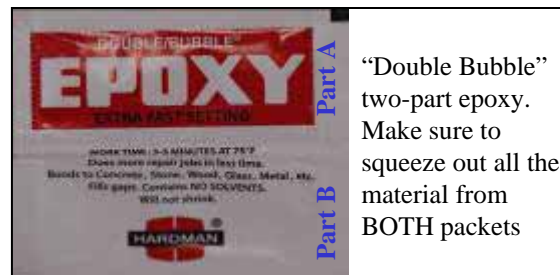
Scarf Joint: Excellent



Single strap joint used to bond toothed belt with Super glue

Structural Joints: *Adhesive*

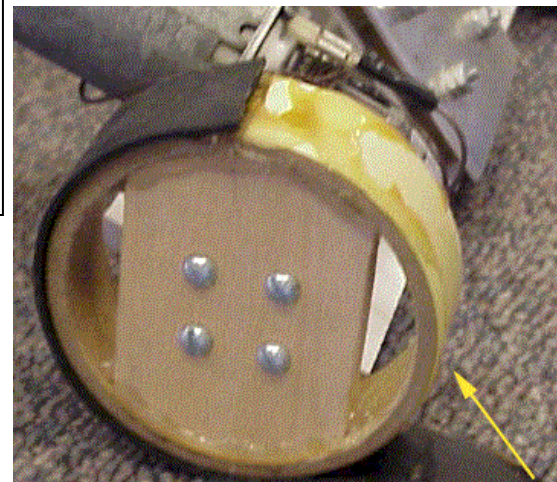
- Adhesives are often used to bond large surface areas
 - Epoxy are often used for making laminates
 - Adhesive joints are usually not meant to be moment connections
 - Thread locking agents are used to keep screw threads from coming undone
 - **CLEANLINESS IS OF UTMOST IMPORTANCE**
 - Check out binding recommendations: <http://www.thisisthat.com/>
- Strengths vary greatly with the type of adhesive, but the lap shear strength is typically are on the order of 15 MPa at 80 °F
 - K. Lewis, “Bonds That Take a Beating”, *Machine Design*, Aug. 8, 2002 pp 69-72



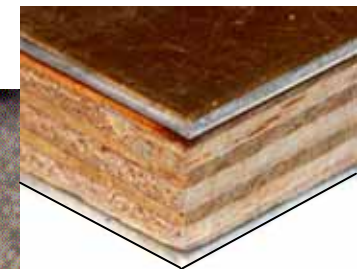
“Double Bubble” two-part epoxy. Make sure to squeeze out all the material from BOTH packets



9-6



Improper surface preparation (rubber should be clean and rough), and the rubber should have been scarf joined



Aluminum epoxied to both sides of plywood which acts as a core

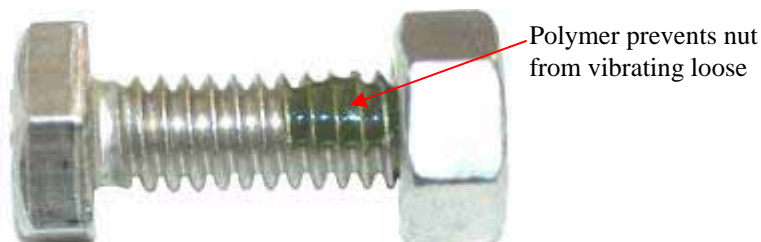
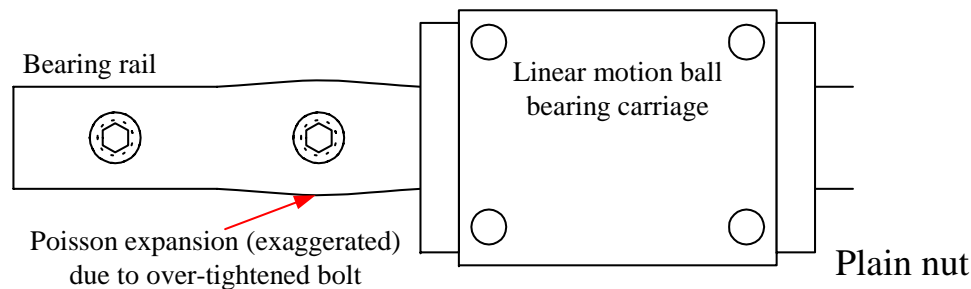
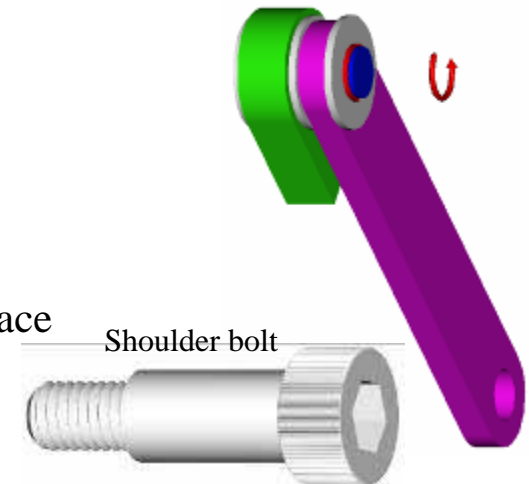


Aluminum epoxied to one side of plywood



Structural Joints: *Bolted*

- Bolts and screws **ONLY** clamp one element to another!
 - Friction and the clamping force are what hold the joint together
 - Washers are used to keep hex-nut edges from chewing up the surface
- Bolts and screws **DO NOT** themselves take shear loads
 - Unless you use a shoulder bolt
- A shoulder bolt can act as a shaft or element of a linkage (pin):
 - When a bolt is to be used to support a bearing, or act as an axle (pin) in a linkage:
 - One end of the bolt must be firmly anchored so it is preloaded and rigid
 - The cantilevered end ideally has a precision ground shoulder that acts as an axle



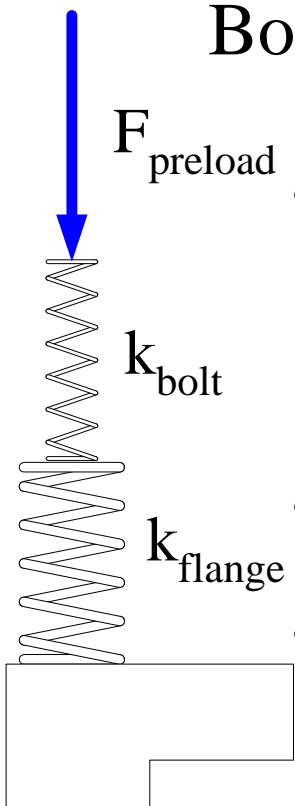
Lock-nut

9-7

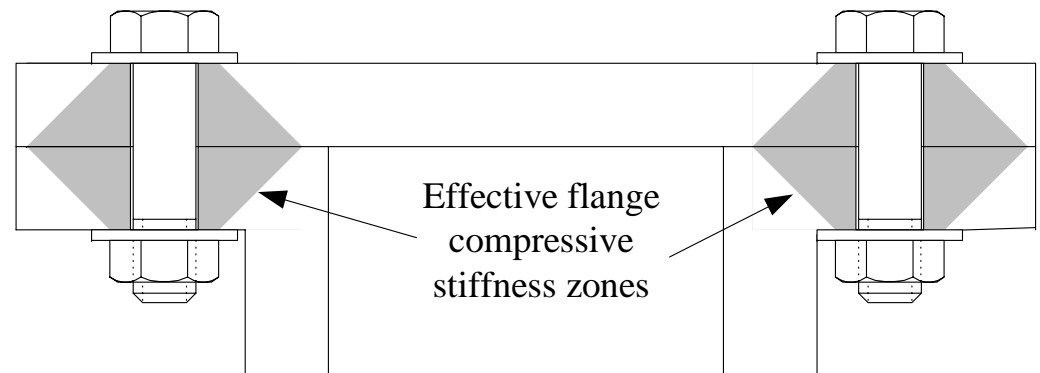
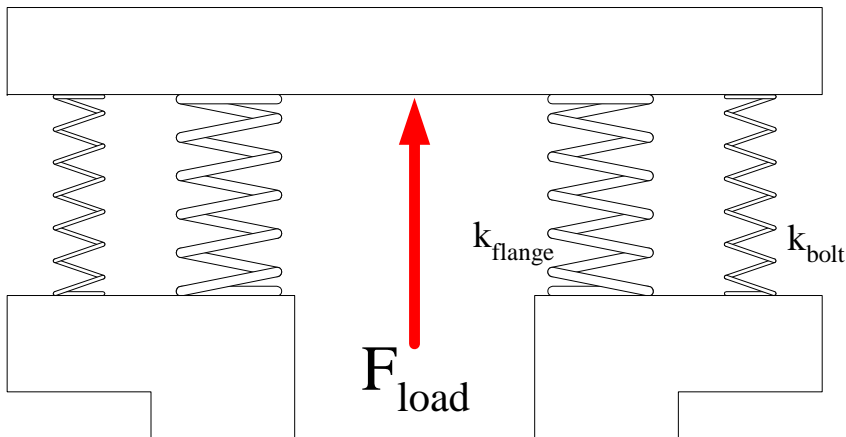
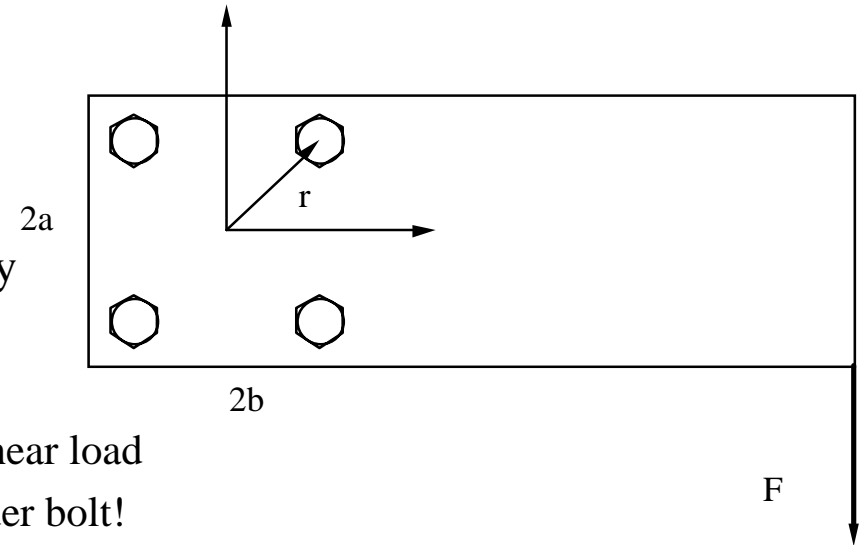


JointCompliance.xls	
Spreadsheet to estimate bevel gear tooth strength	
Production gears must be designed using AGMA standards	
Last modified 9/8/2003 by Alex Slocum	
Enter numbers in BOLD , results in RED	
Be consistant with units! (in, lb or N, m or N, mm)	
Angle of cone of influence, theta (degrees)	45
Diamter of bolt head, Done	20
Diameter of affected zone, Dtwo	32
Thickness of material, t	6
Diameter of bore for bolt, Dbore	12
Modulus of elasticity, E	200000
Compliance, C	3.24941E+07
Stiffness, k	3.08E+06
From FEA	
Load (4x load for quadrant)	1000
displacement	4.55E-04
resulting stiffness, k	2.20E+06
Ktheory/Kfea	1.40
With shear stiffness term (assumes theta = 45 degrees)	
Poisson ratio, n	0.29
Shear stiffness	4216149
Total stiffness (1/(1/compression + 1/shear))	1.78E+06
Ktheory/Kfea	0.81

Bolted Joints: *Mechanics*

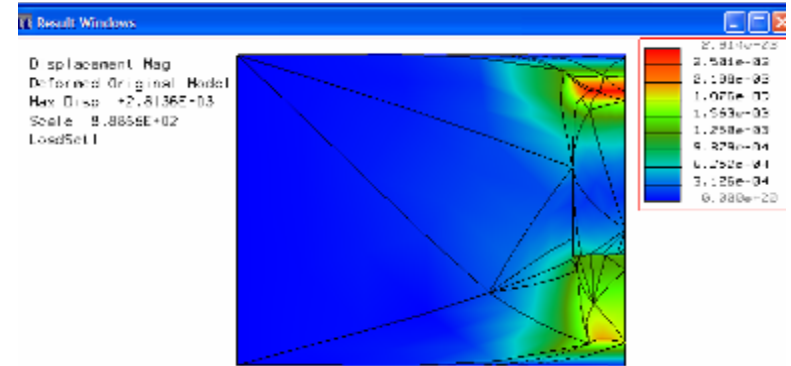


- Bolted joints resist shear **ONLY** by clamping action and friction!
 - Lubrication of threads is critical
 - NEVER rely on a bolt to take a shear load
 - UNLESS the bolt is a shoulder bolt!
- Shear and moment capacity: Find the center of the bolt pattern, and compute the moments about it
- Bolts act in parallel with the stiffness of the joint
 - By tightening them to create a preload higher than the applied load, the effects of alternating stresses created by a load are reduced

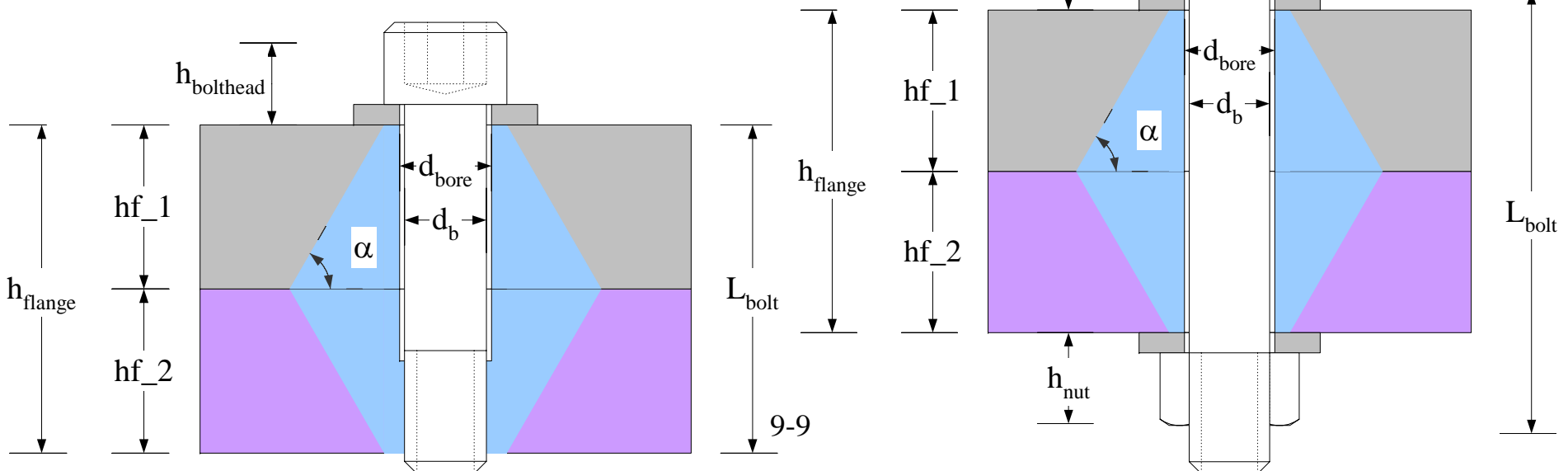


Bolted Joints: *Stiffness*

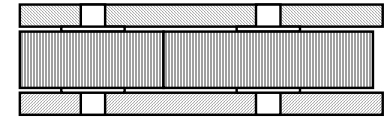
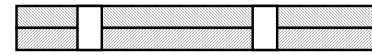
- As bolts are tightened (preloaded), their stiffness acts in series with the flange stiffness
- As external loads are applied to the joint, bolts' stiffness acts in parallel with flange stiffness
- Preloading bolts allows large loads to be applied to a joint while minimally affecting the bolt stress
- A joint can be designed so it “leaks” before a bolt breaks
 - Make the stress cones overlap!
- Bolt_preload.xls* lets you experiment with different dimensions!



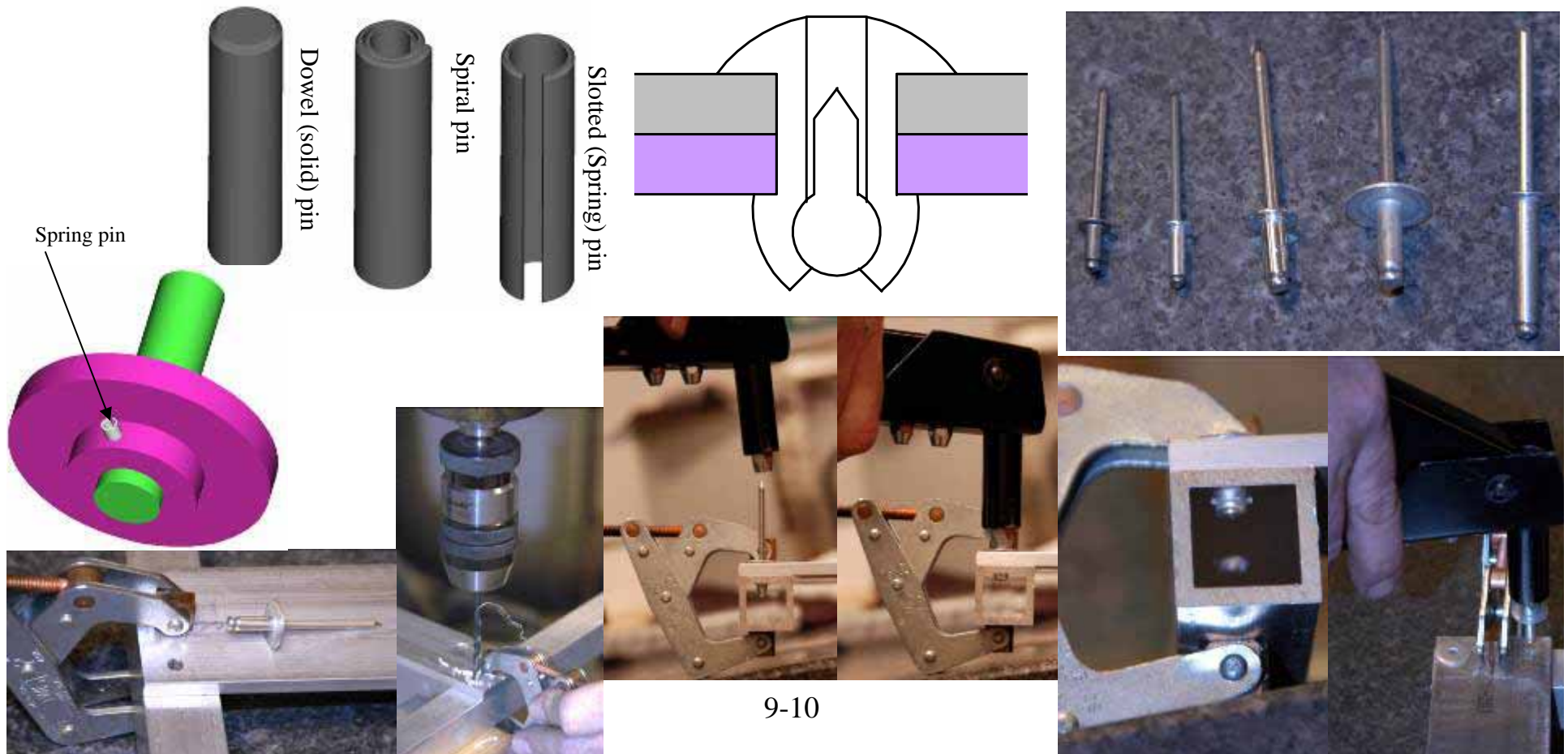
FEA results compared to analysis (60° stress cones)	
Applied load (N)	4000
deflection under bolt head (mm)	0.002810
deflection from threaded region (mm)	0.002100
Total deflection (mm)	0.004910
Stiffness (N/mm)	814664
FEA/Analytical	0.86



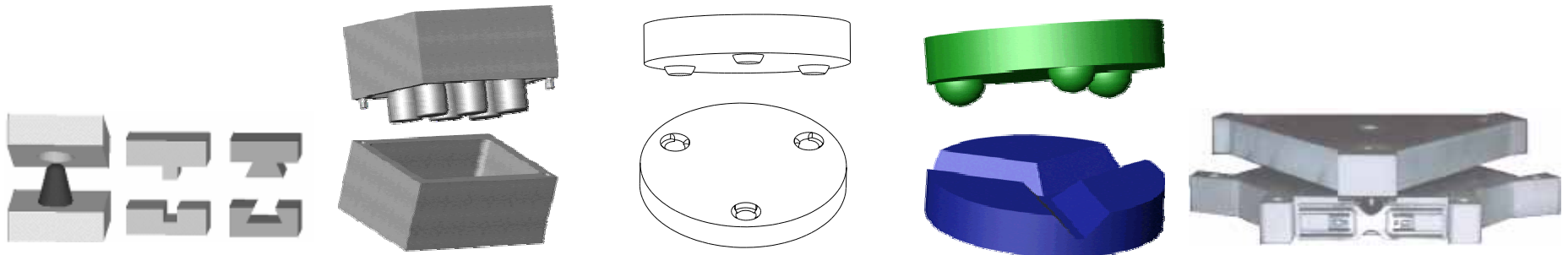
Structural Joints: *Pinned & Riveted*



- Pinned joints use pins pressed into holes to transmit forces (or torque) (see page 5-25)
- Pinning parts together can help during alignment during manufacturing or assembly
 - Line-bore holes for shafts and bearings by pinning plates together and drilling all the holes at once!
- A riveted joint uses expanded members to transmit shear forces and resist peeling forces
 - The expanding nature of the rivet allows many holes to be drilled in parts to be fastened together



Structural Interfaces



Keys

Pinned Joints

Quasi-Kinematic Couplings

Kinematic Couplings

Flexural Kin. Couplings

Over Constrained

Often over Constrained

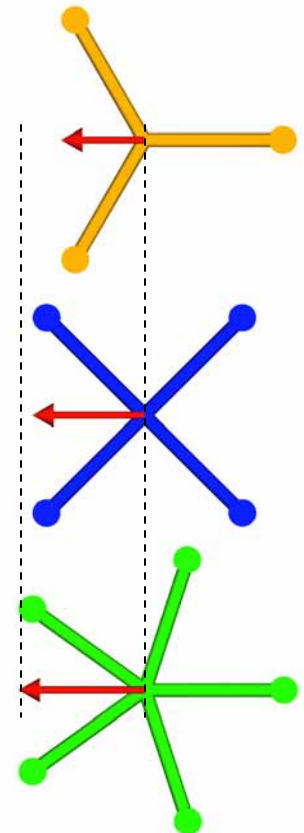
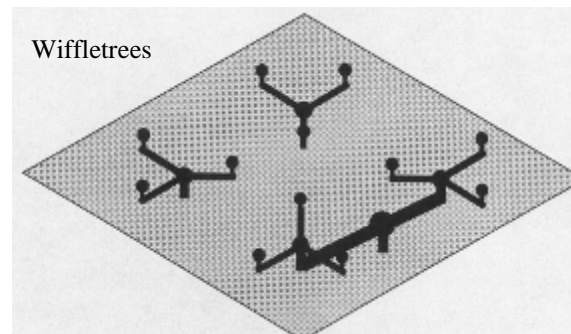
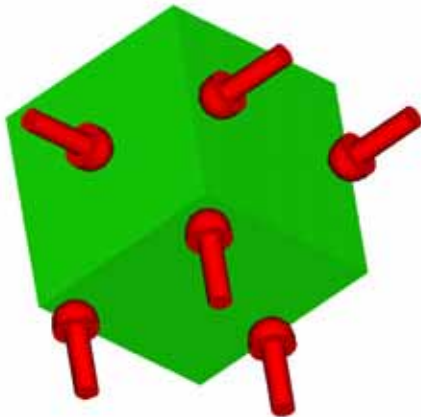
Near Kinematic Constraint

Exact Constraint

Exact Constraint

Repeatability

	0.01 μm	0.10 μm	1.0 μm	10 μm	100 μm
Pinned Joints					
Flexural Kinematic Couplings					
Elastic Averaging					
Quasi-Kinematic Couplings					
Kinematic Couplings					

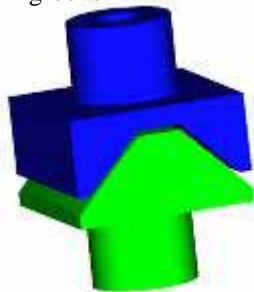


Hertz Contact

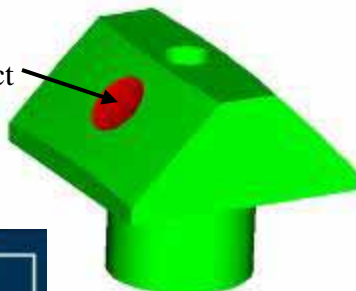
- A most important aspect of interface design are the stresses at the contact points
- In the 1800's, railroad *wheels* were damaging tracks, and rolling element bearing designs were very limited
 - Heinrich Hertz, the mathematician famous for his work in the frequency domain, created the first analytical solution for determining the stress between two bodies in point contact



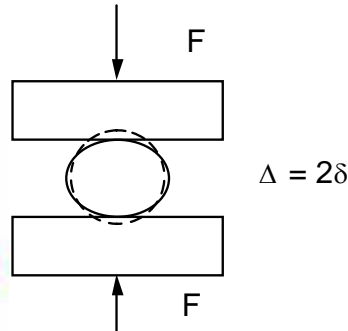
Canoe ball
and vee
groove



Hertz
contact
zone

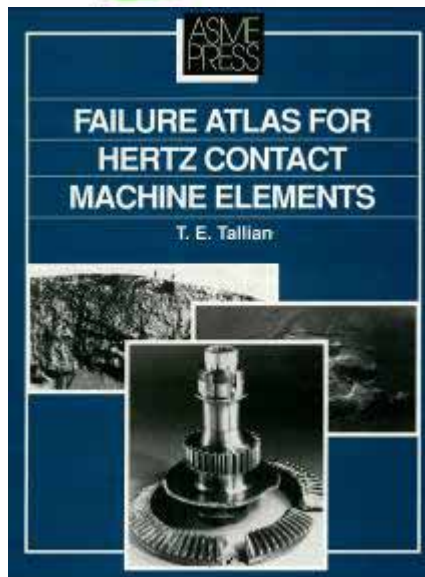


Crowned cone



Heinrich Hertz 1857-1894

9-12



HertzContact.xls	
To determine Hertz contact stress between bodies	
By Alex Slocum, Last modified 1/17/2004 by Alex Slocum	
Last modified 12/28/03 by Alex Slocum	
Enters numbers in BOLD , Results in RED	
Be consistent with units!!	
Ronemaj	1.00E+06
Ronemin	1.00E+06
Rtwomaj	0.500
Rtwomin	0.500
Applied load F	4,358
Phi (degrees)	0
Ultimate tensile stress	3.45E+08
Elastic modulus Eone	1.93E+11
Elastic modulus Etwo	1.93E+11
Poisson's ratio vone	0.29
Poisson's ratio vtwo	0.29
Equivalent modulus Ee	1.05E+11
Equivalent radius Re	0.2500
ellipse c	2.50E-03
ellipse d	2.50E-03
Contact pressure, q	3.33E+08
Stress ratio (must be less than 1)	0.97
Deflection at the one contact interface	
Deflection (μunits)	12.4
Stiffness (load/μunits)	350.8
for circular contact a = c, a	2.50E-03
Depth at maximum shear stress/a	0.634
Max shear stress/ultimate tensile	0.324

Hertz Contact: *Point Contact*

- Equivalent radius R_e and modulus E_e (ν is Poisson ratio):

$$R_e = \frac{1}{\frac{1}{R_{1 \text{ major}}} + \frac{1}{R_{1 \text{ minor}}} + \frac{1}{R_{2 \text{ major}}} + \frac{1}{R_{2 \text{ minor}}}} \quad E_e = \frac{1}{\frac{1-\nu_1^2}{E_1} + \frac{1-\nu_2^2}{E_2}}$$

- $\cos \theta$ (ϕ is the angle between the planes of principal curvature of the two bodies)

$$\cos \theta = R_e \sqrt{\left(\frac{1}{R_{1 \text{ major}}} - \frac{1}{R_{1 \text{ minor}}}\right)^2 + \left(\frac{1}{R_{2 \text{ major}}} - \frac{1}{R_{2 \text{ minor}}}\right)^2 + 2\left(\frac{1}{R_{1 \text{ major}}} - \frac{1}{R_{1 \text{ minor}}}\right)\left(\frac{1}{R_{2 \text{ major}}} - \frac{1}{R_{2 \text{ minor}}}\right)\cos 2\phi}$$

- Elliptic Integrals

$$\alpha = 1.939e^{-5.26\theta} + 1.78e^{-1.09\theta} + \frac{0.723}{\theta} + 0.221$$

$$\beta = 35.228e^{-0.98\theta} - 32.424e^{-1.0475\theta} + 1.486\theta - 2.634$$

$$\lambda = -0.214e^{-4.95\theta} - 0.179\theta^2 + 0.555\theta + 0.319$$

- Major and minor contact area elliptical semi-axes

$$c = \alpha \left(\frac{3FR_e}{2E_e} \right)^{1/3} \quad d = \beta \left(\frac{3FR_e}{2E_e} \right)^{1/3}$$

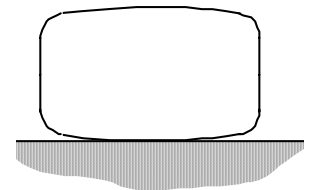
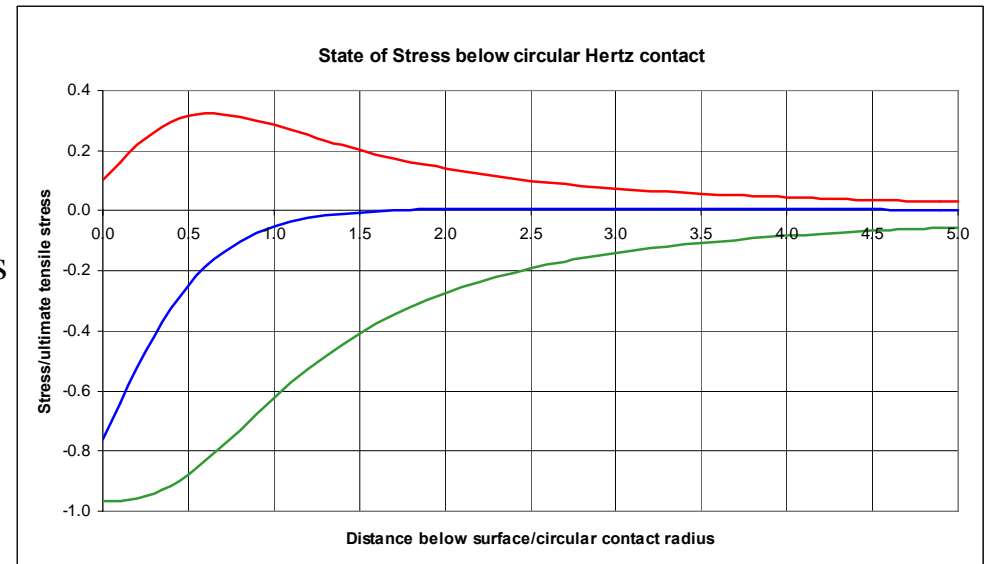
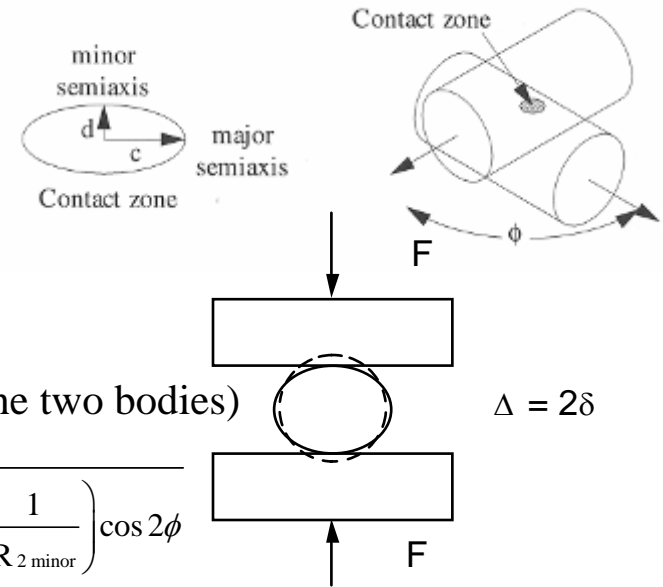
- Contact pressure & Deflection

$$q = \frac{3F}{2\pi cd} \leq 1.5\sigma_{\text{for metals, ultimate tensile strength}} \quad \delta = \lambda \left(\frac{2F^2}{3R_e E_e^2} \right)^{1/3}$$

- State of stress for circular contact of radius a as a function of depth z below the surface

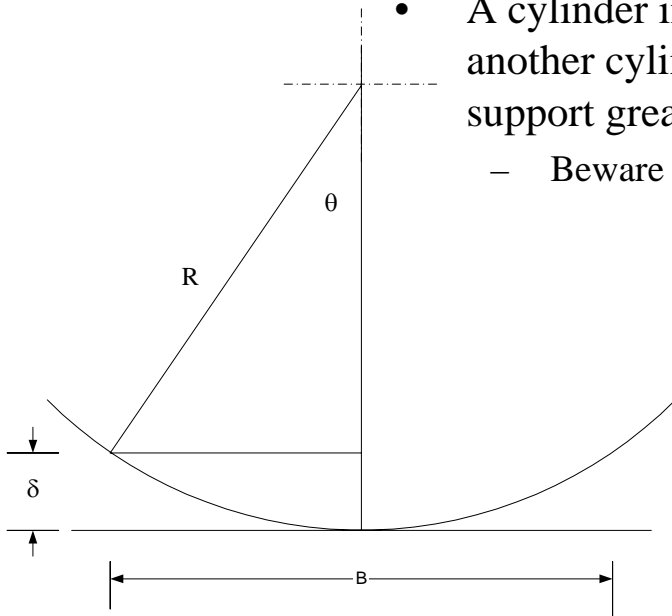
$$\sigma_z(z) = q \left(-1 + \frac{z^3}{(a^2 + z^2)^{1.5}} \right) \quad \sigma_r(z) = \sigma_\theta(z) = \frac{q}{2} \left(-(1+2\nu) + \frac{2(1+\nu)z}{\sqrt{a^2 + z^2}} - \frac{z^3}{(a^2 + z^2)^{1.5}} \right) \quad \tau(z) = \frac{\sigma_\theta(z) - \sigma_z(z)}{2}$$

9-13

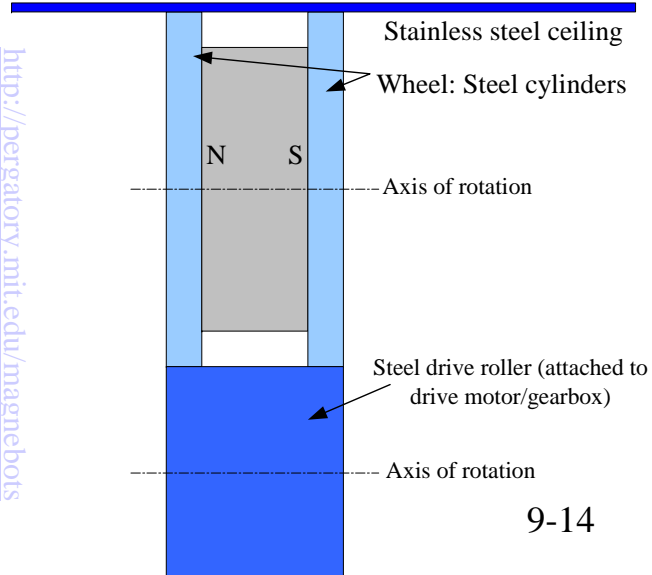


Hertz Contact: *Line Contact*

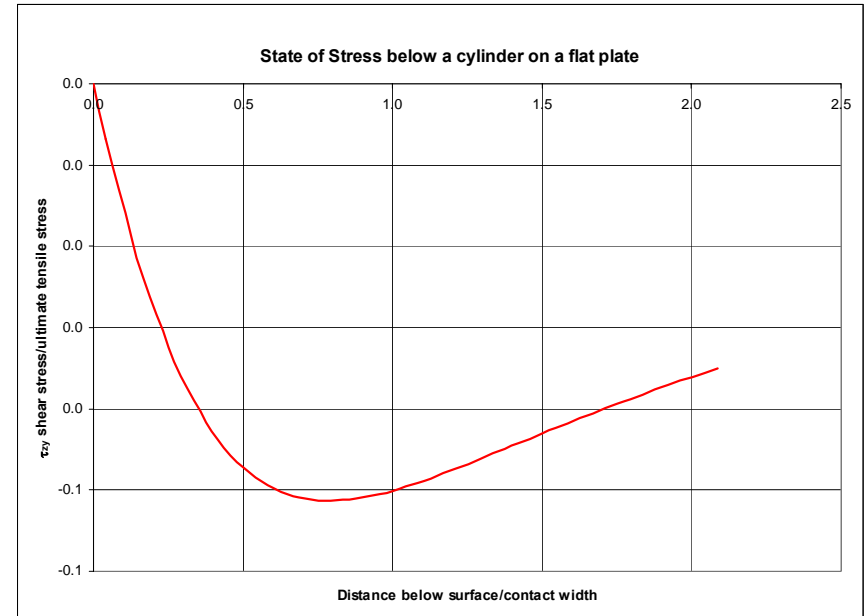
- A cylinder in contact with another cylinder or a plate can support great forces
 - Beware of edge loading!



<http://pergatory.mit.edu/magnebots>



9-14



Hertz_contact_line.xls

To determine Hertz contact stress between two cylinders

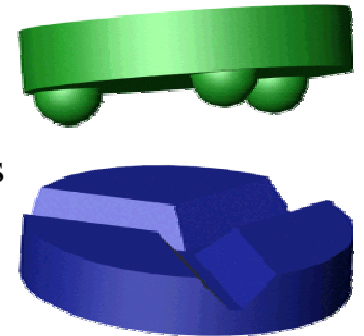
By Alex Slocum, last modified 2/10/2004 by Alex Slocum

Enters numbers in **BOLD**, Results in **RED**

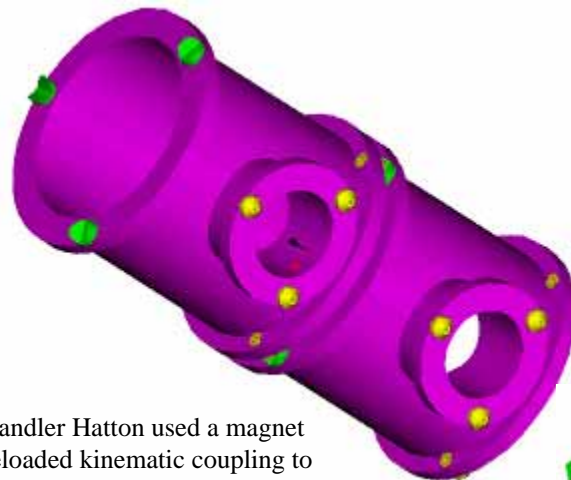
Smaller cylinder 1 diameter, d_1 (mm)	10
Larger cylinder 2 (or flat plane) diameter, d_2 (mm)	100
Length, L (mm)	10
Applied load, F (N)	8,184
Elastic modulus Eone (N/mm^2)	2.00E+05
Elastic modulus Etwo (N/mm^2)	2.00E+05
Poisson's ratio vone	0.29
Poisson's ratio vtwo	0.29
Ultimate tensile stress, sigult (N/mm^2)	1500
Depth below contact surface for evaluating deflection, do	300
Rectangular contact zone width, 2b (mm)	0.42
Contact pressure, qcy1 (N/mm^2)	2502
Deflection motion of d_1 center, defl_1 (mm)	0.0104
Deflection motion of d_2 center, defl_2 (mm)	0.013159
Total relative displacement of the cylinder's centers, dcyls (mm)	0.0236
Stress factor: Must be less than 1	
Maximum shear stress/(ultimate tensile/2)	1.00
Manufacturing issues	
Surface roughness, Ra (mm)	0.005
Potential induced contact width, Bra (mm)	0.4

Kinematic Couplings

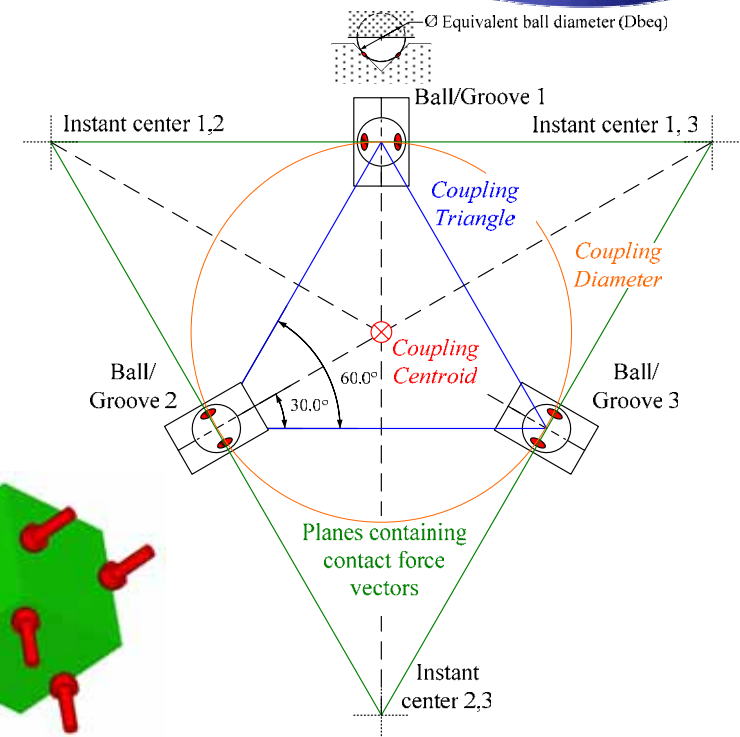
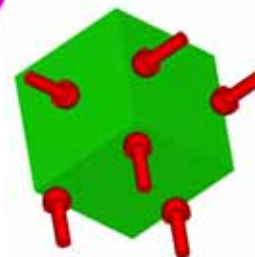
- When a component is constrained by a number of points equal to the number of degrees of freedom, it is said to be *exactly constrained*
 - Kinematics is the study of motion, assuming bodies are rigid, so when a design is “kinematic” it means it is exactly constrained, and geometric equations can be written to describe its motion
- Kinematic Couplings are couplings that exactly constrain components
 - They are not stable unless ALL six contact points are engaged
 - There are no intermediate stability configurations like those in 3-2-1 couplings
 - They can provide repeatability on the order of parts' surface finish
 - $\frac{1}{4}$ micron repeatability is common
- Managing the Hertz contact stresses!

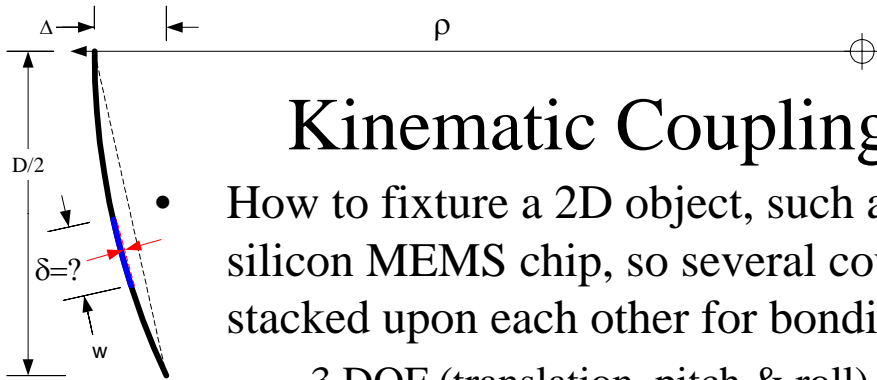


Chandler Hatton used a magnet preloaded kinematic coupling to enable her machine's module to be easily flipped depending which side of the table on which she had to setup



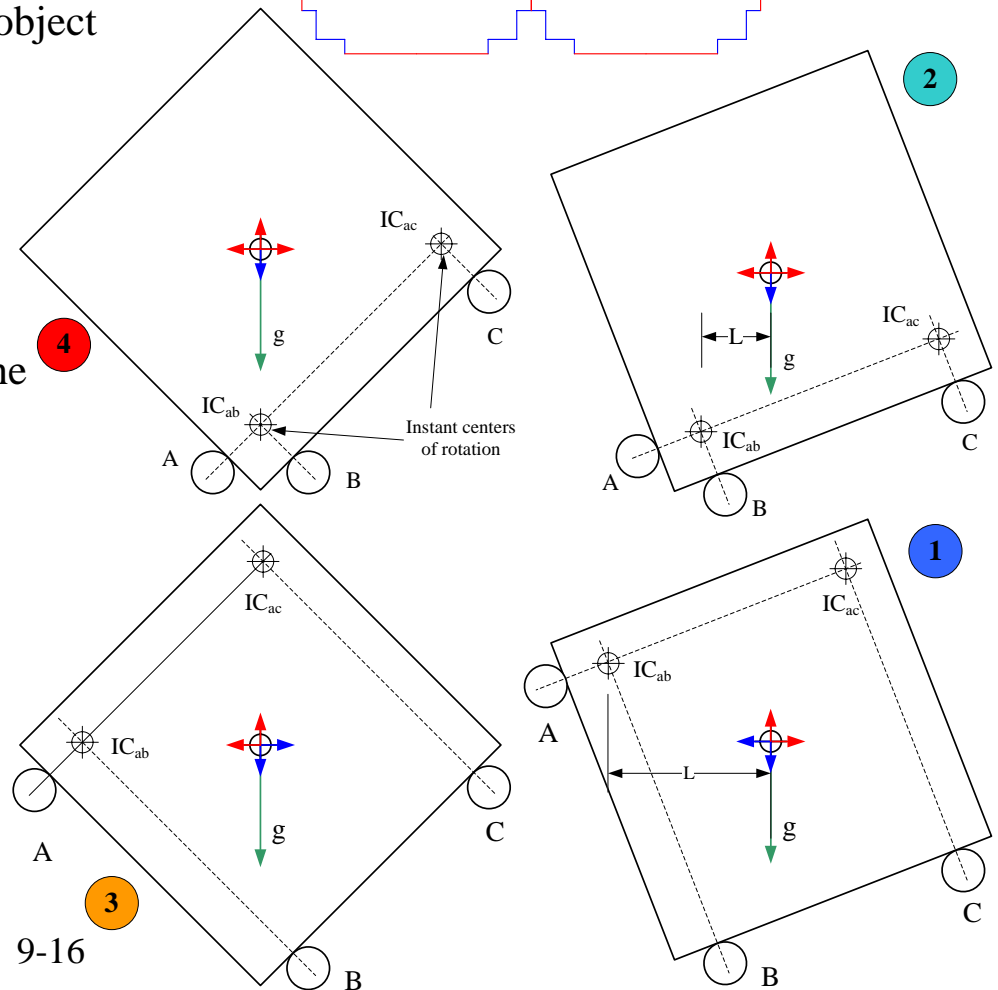
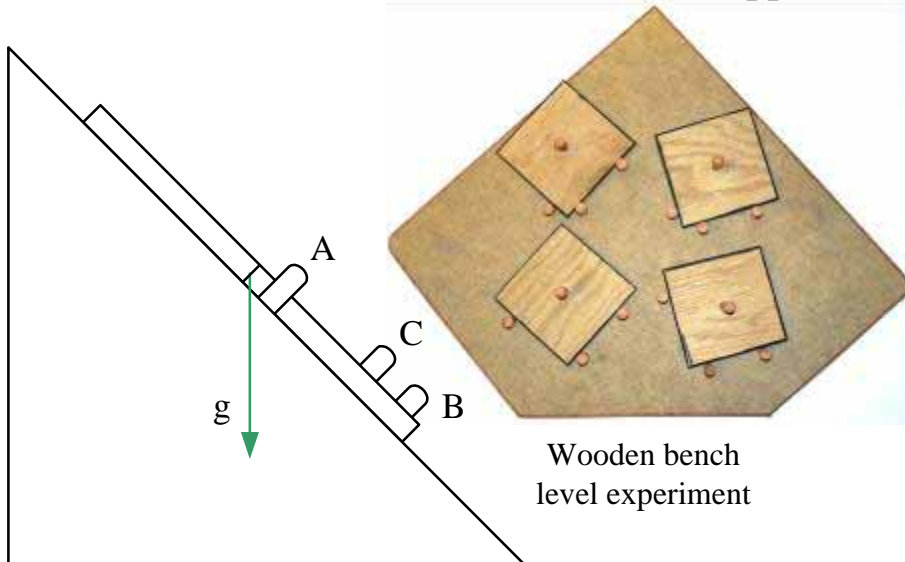
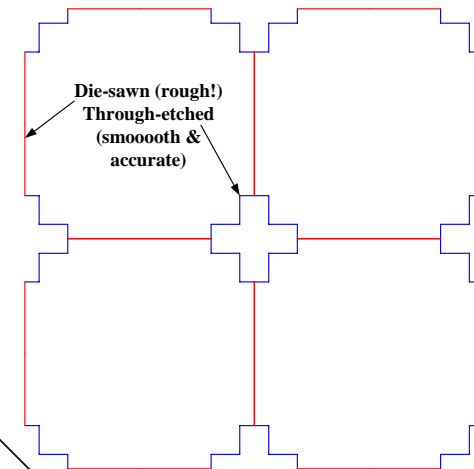
9-15





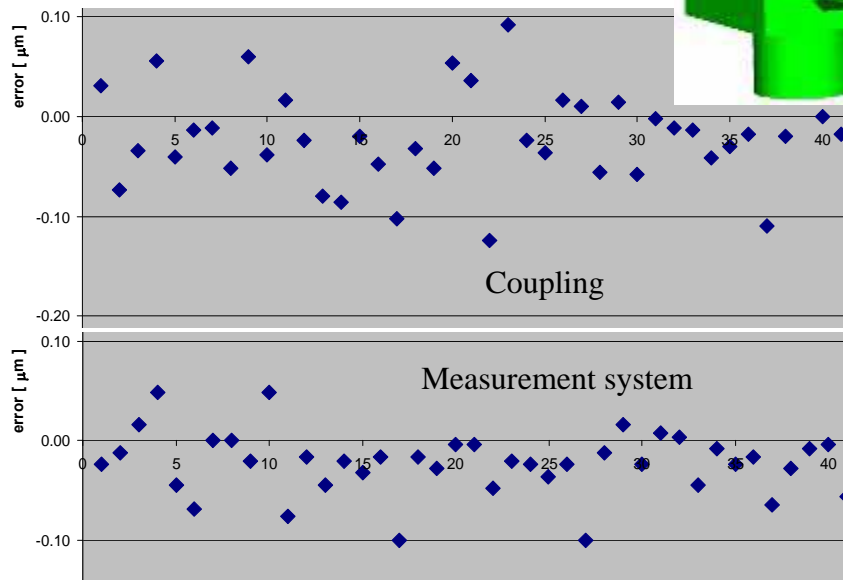
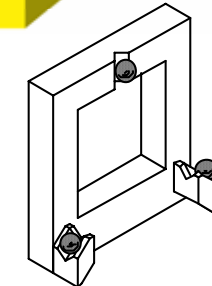
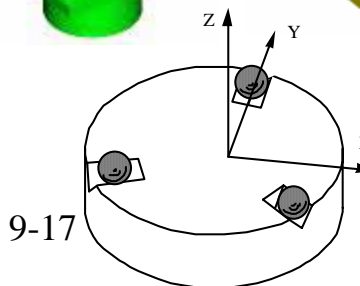
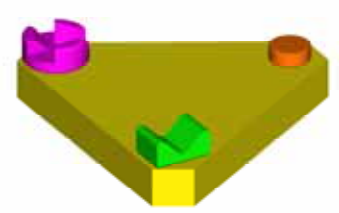
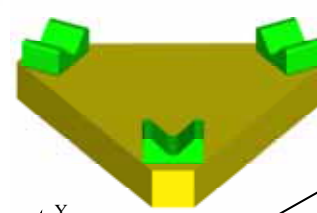
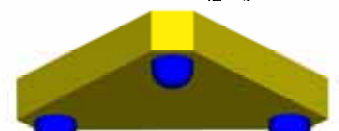
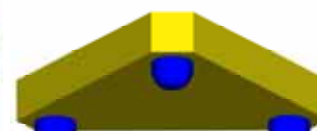
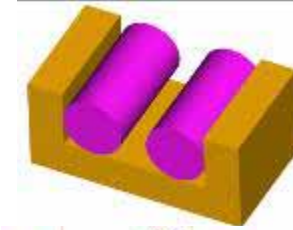
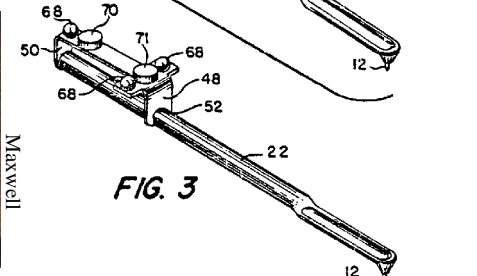
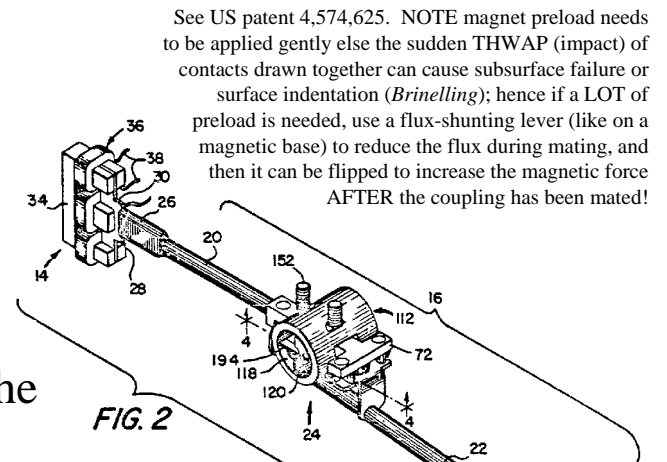
Kinematic Couplings: 2D

- How to fixture a 2D object, such as a silicon MEMS chip, so several could be stacked upon each other for bonding?
 - 3 DOF (translation, pitch & roll) are defined by the plane on which the object rests
 - 3 DOF (2 translations and yaw) must be established
 - 3 contact points are needed
 - Gravity provides preload
 - Align the gravity vector wrt the instant centers of support



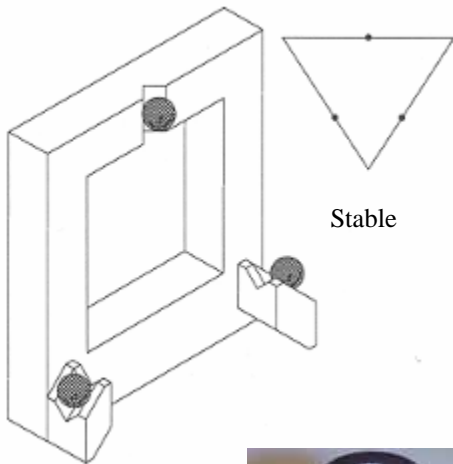
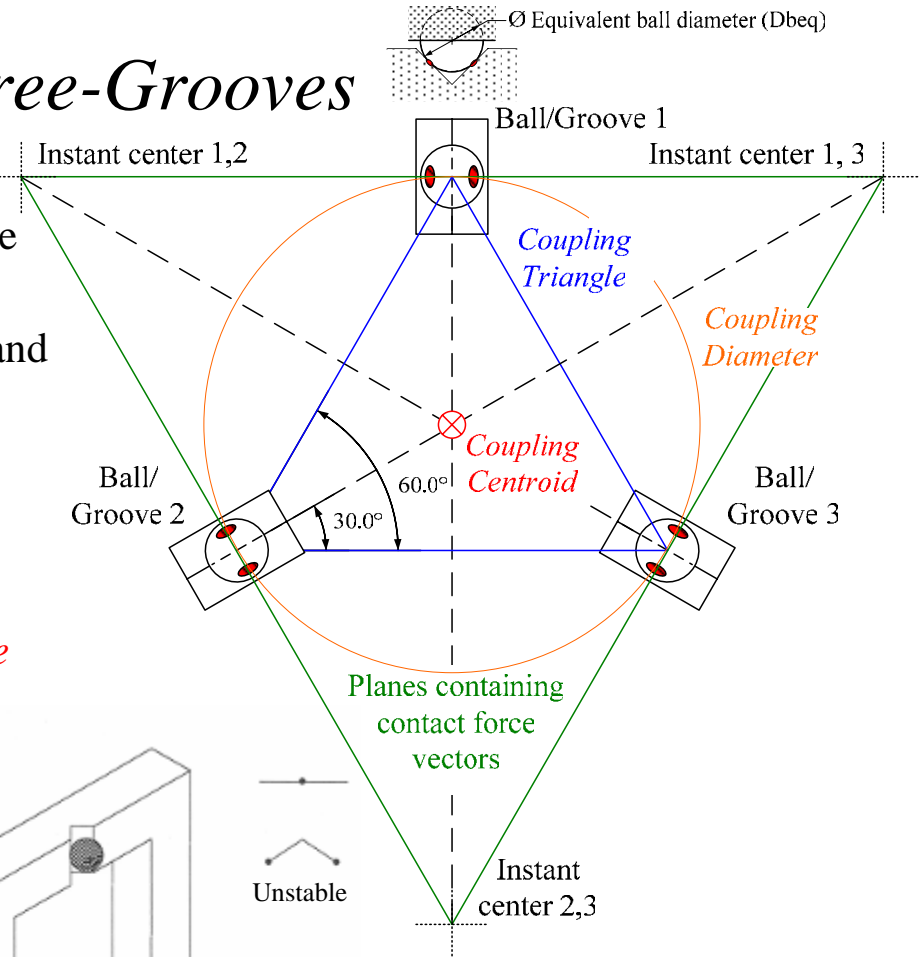
Kinematic Couplings: 3D

- James Clerk Maxwell (1831-1879) liked the three-grooves
 - Symmetry good for manufacture, dynamic stability
 - Easy to obtain very high load capacity
- William Thomson (later Lord Kelvin) (1824 - 1907) liked the ball-groove-tetrahedron
 - More intuitive, and applicable to non-planar designs

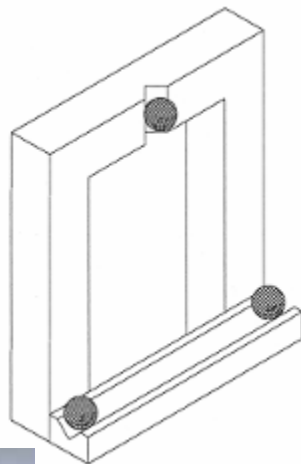


Kinematic Couplings: *Three-Grooves*

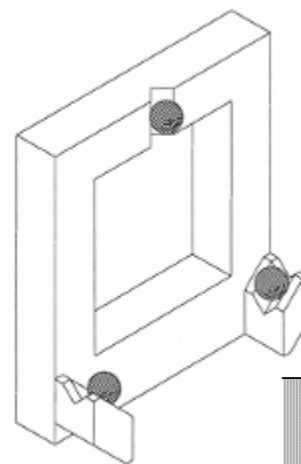
- For long life, Hertz contact pressure $q < \sigma_{yield}$
 - Contact area center should not be closer than one contact ellipse diameter from groove edge
 - Materials must be non-galling (no AL on AL!) and non-fretting
 - Preload to keep coupling from tipping
- *Ideally align the grooves with the coupling triangle's angle bisectors*
 - *The coupling centroid will NOT always be at the coupling triangle centroid!*



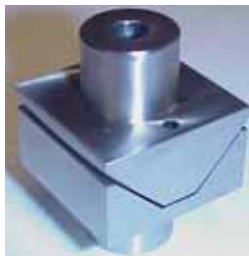
Stable



Neutral

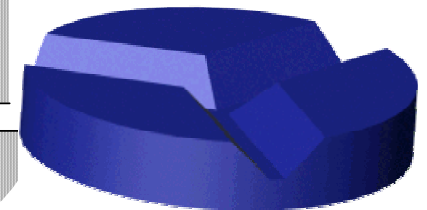
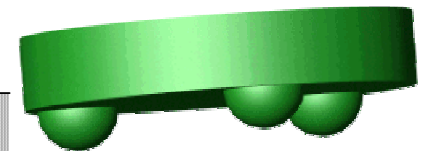


Unstable



See www.kinematiccouplings.org for spreadsheets, articles, and suppliers

Don't forget the potential of using magnets for light load applications!

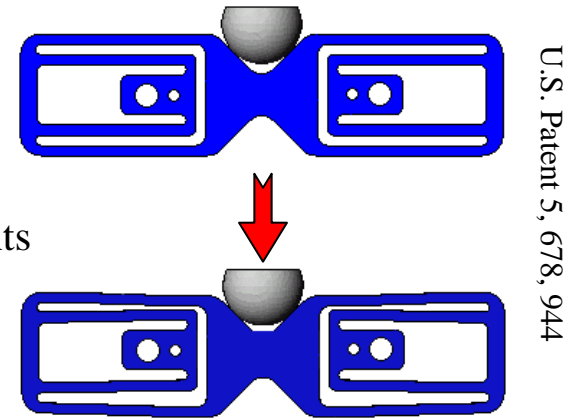


Kinematic Couplings: *Three-Grooves*

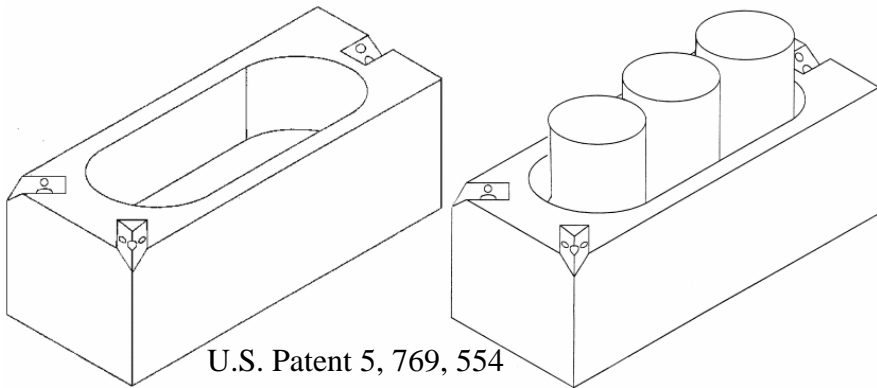
Kinematic_Coupling_3Groove_Design.xls					
To design three groove kinematic couplings					
Written by Alex Slocum. Last modified 10/27/2004 by Alex Slocum					
Metric units only! Enters numbers in BOLD , Results in RED				Material properties	
Standard 120 degree equal size groove coupling? (contact forces are inclined at 45 to the XY plane. For non standard designs, enter geometry after results section)		TRUE	<i>User defined material</i>		<i>aluminum</i>
			<i>Yield stress</i>		
System geometry (XY plane is assumed to contain the ball centers)				plastic	3.45E+07
Dbeq (mm) =	5	Equivalent diameter ball to contact the groove at the same points		RC 62 Steel	1.72E+09
Rbminor (mm) =	2.5	"Ball" minor radius		CARBIDE	2.76E+09
Rbmajor (mm) =	2.5	"Ball" major radius		user defined	2.76E+08
Rgroove (mm) =	1.00E+06	Groove radius (negative for a trough)		<i>Elastic modulus</i>	
Costheta =	TRUE	Is ball major radius along groove axis?		plastic	2.07E+09
Dcoupling (mm) =	150	Coupling diameter		RC 62 Steel	2.04E+11
Fpreload (N) =	-100	Preload force over each ball		CARBIDE	3.10E+11
Xerr (mm) =	0.0	X location of error reporting		user defined	6.80E+10
Yerr (mm) =	0.0	Y location of error reporting		<i>Poisson ratio</i>	
Zerr (mm) =	0.0	Z location of error reporting		plastic	0.20
Auto select material values (enter <i>other_4</i> to the right)				RC 62 Steel	0.29
Matlabball =	1	Enter 1 for plastic, 2 for steel, 3 for carbide, 4 for user defined, 5 where each ball and groove is defined individually		CARBIDE	0.30
Matlabgroove =	4			user defined	0.29
Min. yield strength (Pa, psi)		3.45E+07	5,000		
Largest contact ellipse major diameter (mm)		0.831			
Largest contact ellipse major diameter (mm)		0.829			
Largest contact stress ratio		3.826	Max Hertz shear stress/Material's max shear stress (tensile yield/2)		
RMS applied force F (N)	17.32				
RMS deflection at F (micron)	2.238				
RMS stiffness (N/micron)	7.74				
Applied force's Z,Y,Z values and coordinates			Coupling centroid location		
FLx (N) =	10.00	XL (mm) =	0	xc (mm)	0.000
FLy (N) =	10.00	YL (mm) =	0	yc (mm)	0.000
FLz (N) =	10.00	ZL (mm) =	100	zc (mm)	0.000

Kinematic Couplings: *Compliant Mounts*

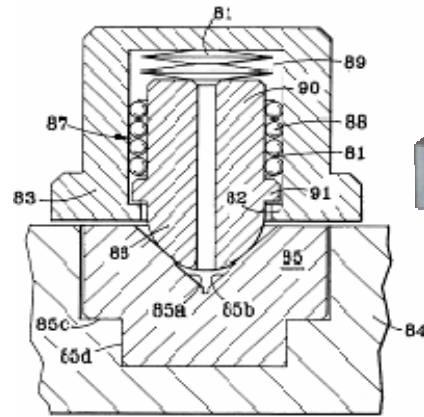
- Allows a component to be kinematically located
 - Application of the preload force deflects the kinematic components until surface-to-surface contact occurs to resist tipping loads
- Many forms from simple sheet metal to flexure-based linkages
- Deformation can be elastic, or permanent
 - Even sand cores can be aligned



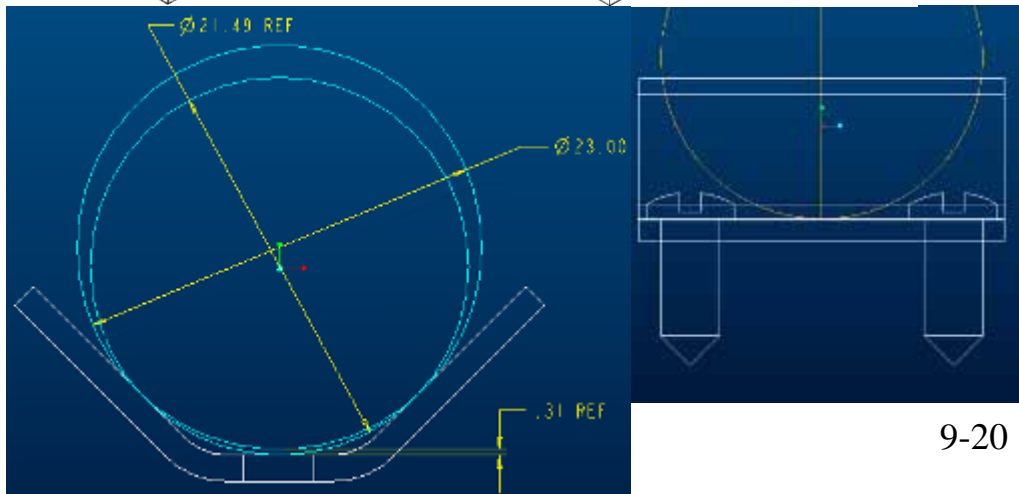
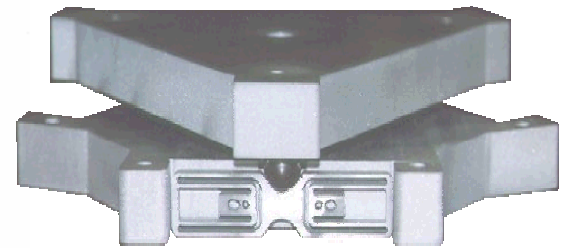
U.S. Patent 5, 678, 944



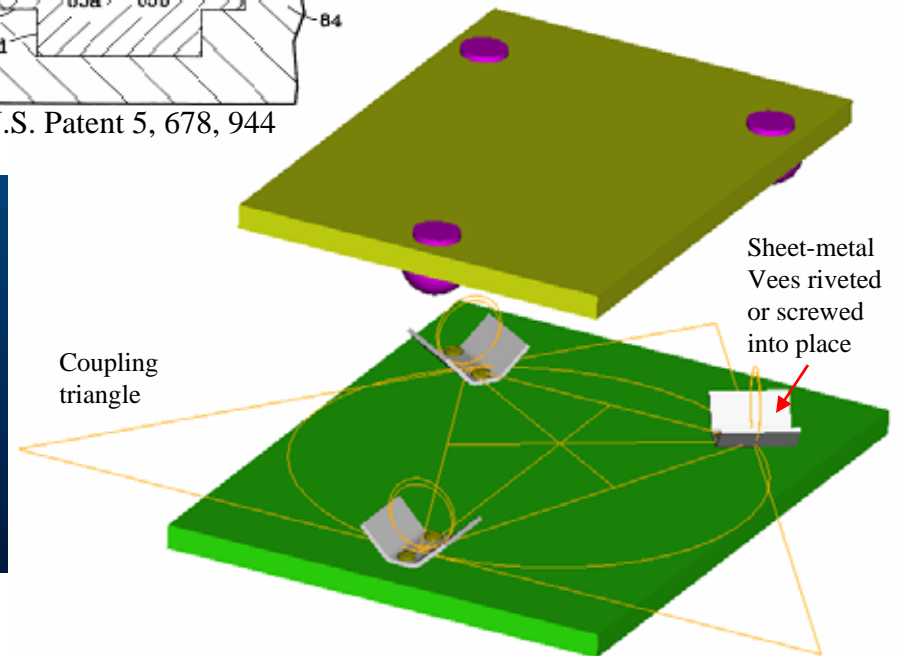
U.S. Patent 5, 769, 554



U.S. Patent 5, 678, 944

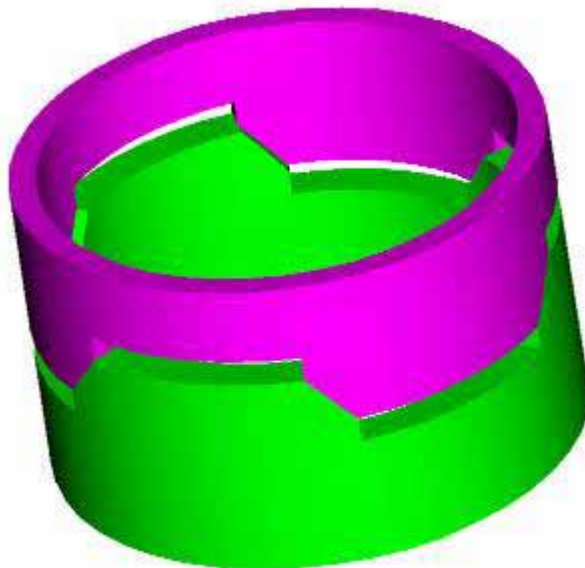


9-20



Kinematic Couplings: *Three-Tooth*

- A semi-kinematic effect can be achieved by having three teeth each on two coupling halves mate at six points
 - 3-5 micron repeatability can be obtained with this simple design
- Layton Hale at LLNL put crowns on one set of the teeth to create a nearly true kinematic three tooth coupling:
 - 1 micron repeatability can be obtained with this simple design



United States Patent [19] **Patent Number:** 6,065,898
Hale [45] **Date of Patent:** *May 23, 2000

[54] THREE TOOTH KINEMATIC COUPLING

[75] Inventor: **Layton C. Hale**, Livermore, Calif.

[73] Assignee: **The Regents of the University of California**, Oakland, Calif.

[*] Notice: Under 35 U.S.C. 154(b), the term of this patent shall be extended for 634 days.

[21] Appl. No.: **08/511,980**

[22] Filed: **Aug. 7, 1995**

[51] Int. Cl.⁷ **F16D 1/00**

[52] U.S. Cl. **403/364; 403/190; 403/340; 403/381; 464/157; 192/69.83**

[58] Field of Search 403/190, 291, 403/364, 311, 340, 381; 192/114 T, 69.81, 69.82, 69.83; 464/149, 157

[56] References Cited

U.S. PATENT DOCUMENTS

1,241,118 9/1917 Hoskins 464/157
 1,260,690 3/1918 Liady 403/364 X
 1,739,756 12/1929 Granville 464/149
 2,094,416 9/1937 Sheffield 403/364 X
 2,384,583 9/1945 Wildhaber 192/69.83
 2,388,456 11/1945 Wildhaber 464/157 X
 2,398,570 4/1946 Wildhaber 403/364 X
 2,551,735 5/1951 Goff 464/149
 2,654,456 10/1953 Wildhaber 192/69.83 X
 4,074,946 2/1978 Swearingen 403/364
 4,307,795 12/1981 Roy 192/69.82
 5,730,657 3/1998 Olgren 464/157

FOREIGN PATENT DOCUMENTS

850296 12/1939 France 403/364
 14963 7/1969 Japan 464/157
 578287 6/1946 United Kingdom 464/157

OTHER PUBLICATIONS

A. Slocum, Precision Machine Design, Prentice Hall, 1992, pp. 401-402.
 D.L. Blanding, Principles of Exact Constraint Mechanical Design, Eastman Kodak Co., 1992, pp. 28-29.
 Machinery handbook, 24th Edition, Couplings and Clutches, Industrial Press, 1992, pp. 2237-2239.

Primary Examiner—Daniel P. Stodola

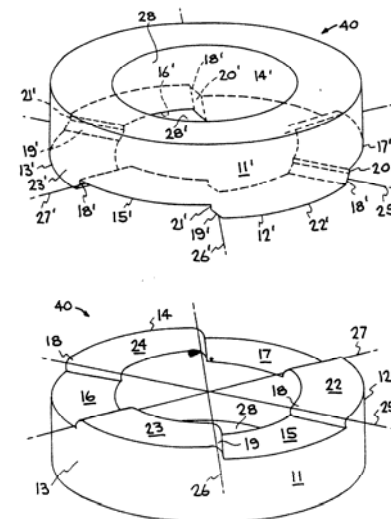
Assistant Examiner—Bruce A. Lev

Attorney, Agent, or Firm—Alan H. Thompson; L. E. Carnahan

[57] ABSTRACT

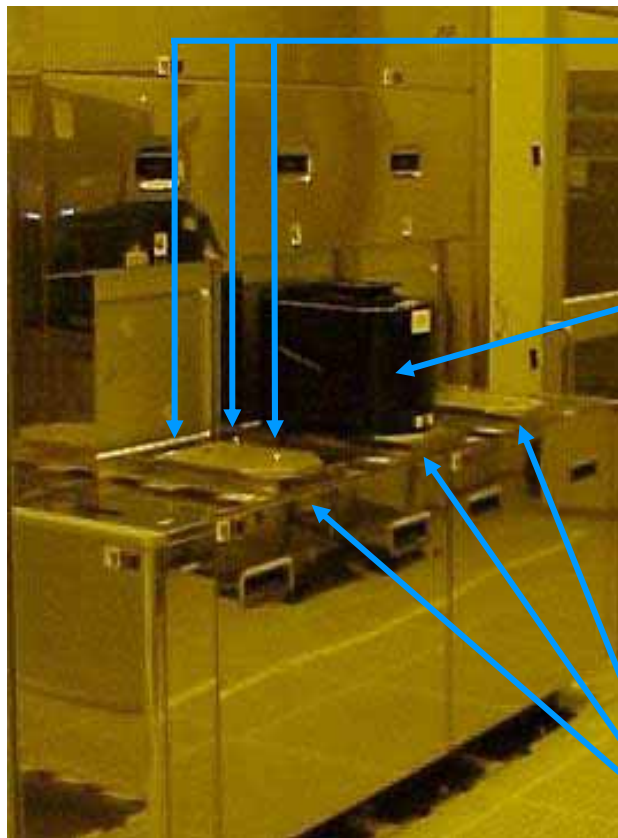
A three tooth kinematic coupling based on having three theoretical line contacts formed by mating teeth rather than six theoretical point contacts. The geometry requires one coupling half to have curved teeth and the other coupling half to have flat teeth. Each coupling half has a relieved center portion which does not effect the kinematics, but in the limit as the face width approaches zero, three line contacts become six point contacts. As a result of having line contact, a three tooth coupling has greater load capacity and stiffness. The kinematic coupling has application for use in precision fixturing for tools or workpieces, and as a registration device for a work or tool changer or for optics in various products.

15 Claims, 2 Drawing Sheets



Kinematic Couplings: 300mm Wafer Transport

- How to precisely locate a plastic wafer carrying structure (FOUP) on a tool, so a robot can precisely load/unload wafers?
 - Exactly constrain it of course with an interface that contacts the FOUP at 6 unique points!
 - BUT success requires careful management of contact stresses, and development of standards upon which manufacturers can agree

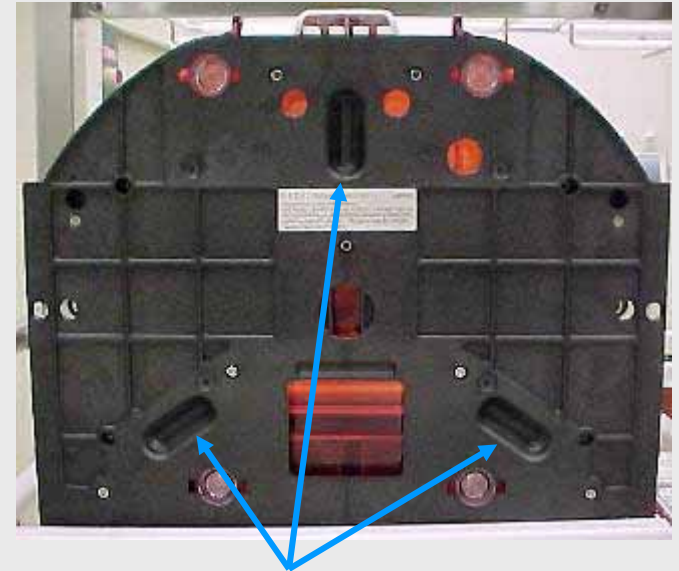


Kinematic coupling pins on loadport based on SEMI E57 standard

300mm Wafer carrier (FOUP) precisely positioned on kinematic coupling pins on loadport

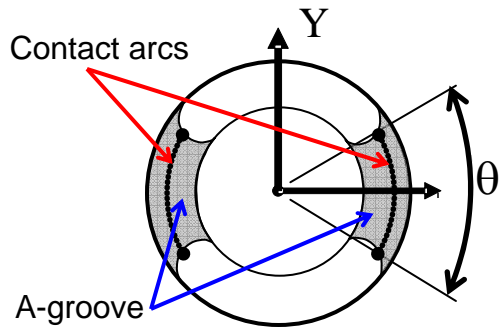
Production equipment loadports based on SEMI E15.1 standard

Base of the FOUP



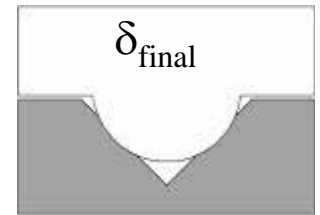
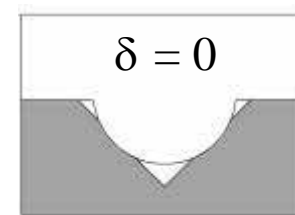
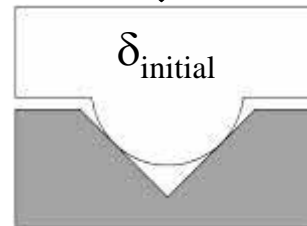
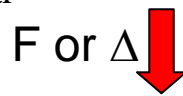
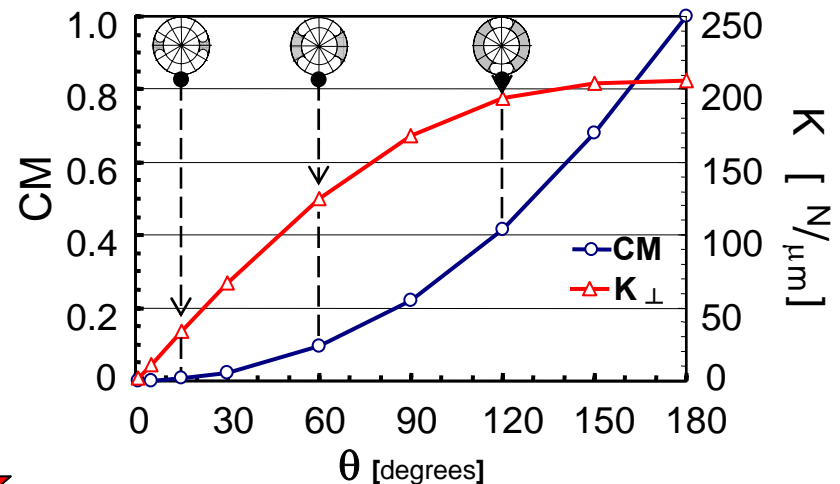
Mating kinematic coupling grooves on the FOUP, permitting precise alignment on load ports, so robots can precisely access 300 mm wafers

Quasi-Kinematic Couplings



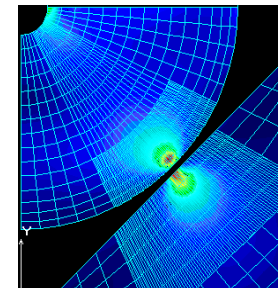
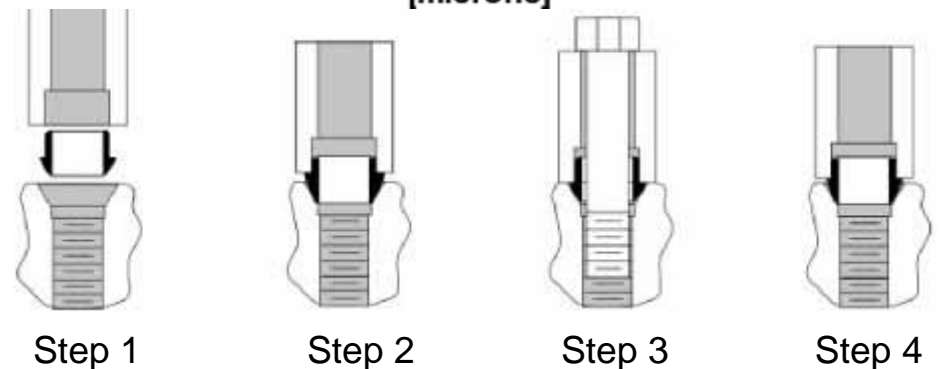
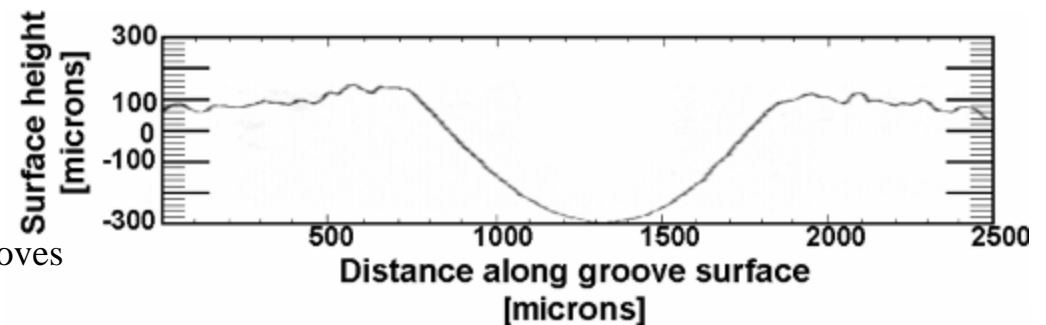
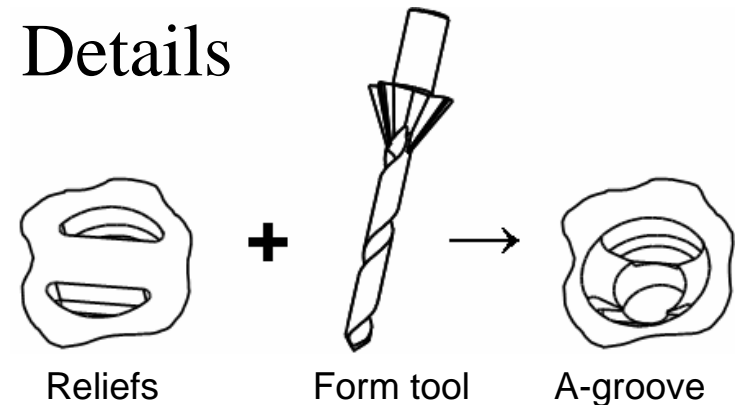
- **KC geometry**
 - 3 balls (hemispheres)
 - 3 *v-grooves*
 - 6 “point” contacts
- **QKC geometry**
 - 3 balls (hemispheres)
 - 3 *A-grooves* (surface of revolution)
 - Circular arc contact
 - Remove groove material to form arc contacts
- **Ideal constraint:**
 - Desire all constraints to be perpendicular to bisectors of triangle angles
 - Desire no constraint parallel to bisectors of triangle vertices
 - Constraint metric (CM) = $\frac{\text{constraint parallel}}{\text{constraint perpendicular}}$
 - Ideal CM = 0
- **QKCs are weakly over constrained**
 - Contact angle q defines arc geometry
 - Larger θ = stiffer joint but more over constraint
 - Choose design which delivers adequate stiffness, K , and minimizes CM
 - $\theta < 60$ degrees typically emulate a true kinematic coupling

	Kinematic coupling	QKCs
Coupling geometry		
Coupling constraints		



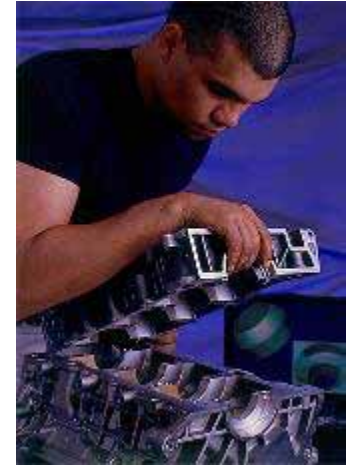
Quasi-Kinematic Couplings: Details

- **Fabricating QKC geometry**
 - Pre-cast or machine reliefs
 - Form tool machines axisymmetric *A-grooves*
 - Balls can be ball bearings or may be ground
- **QKC mating cycle**
 - Step 1: Balls are assembled into top part
 - Step 2: Balls mate A-grooves; finite gap between components
 - Step 3: Balls are preloaded into A-grooves
 - Gap is closed allowing interface to seal
 - Step 4: When preload is released, balls and grooves elastically recover
- **Ball and groove deformation**
 - During Step 3, grooves plastically deform
 - Plastic deformation reduces mismatch between ball and groove patterns
 - Balls and grooves elastically recover in Step 4
 - Recovery restores gap between parts
- **Surface finish**
 - Repeatability of coupling scales as $1/3$ RA
 - Rough finish = poor repeatability
 - Grinding and/or polishing are expensive
 - Press hard, fine-surfaced ball surface into rough groove surface

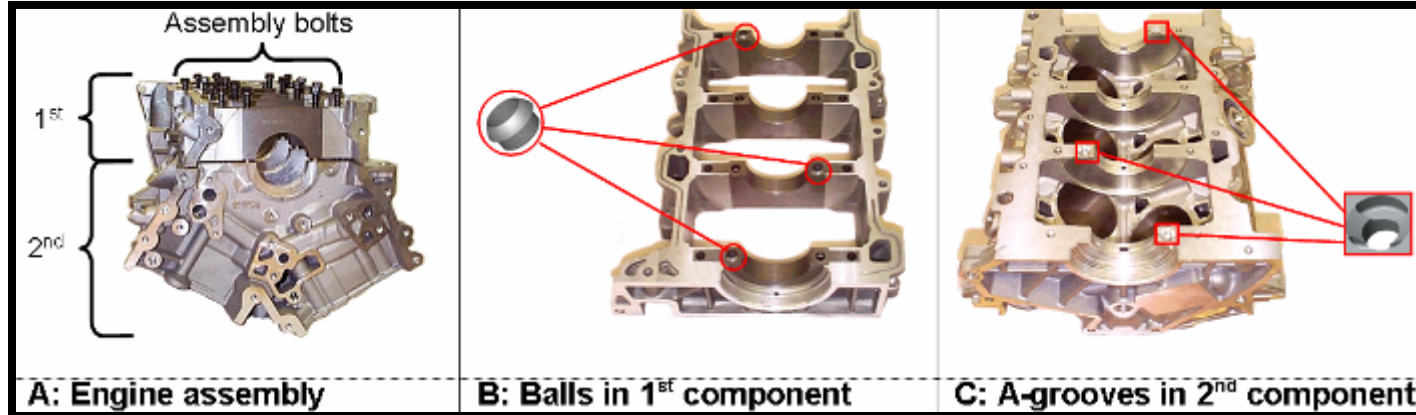


Quasi-Kinematic Couplings: Automotive Example

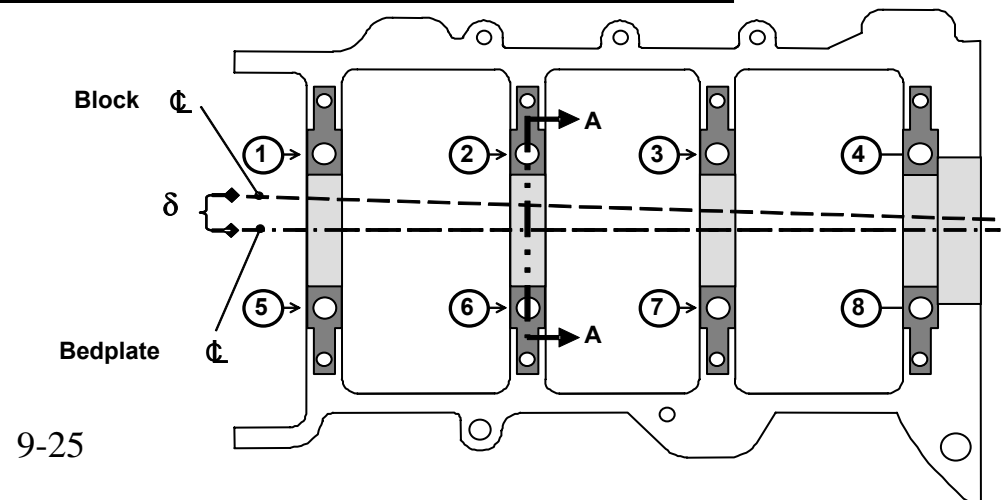
- Original alignment design
 - Components were aligned with 8 pin-hole joints
 - This design is very over constrained
 - Pin-hole patterns requires tight tolerances
 - 8 precision ground dowels required
 - 16 precision holes are bored
- QKC design
 - 8 pins => 3 balls
 - 16 holes =>
 - 3 holes
 - 3 A-grooves



Prof. Martin Culpepper with his Ph.D. thesis, the QKC

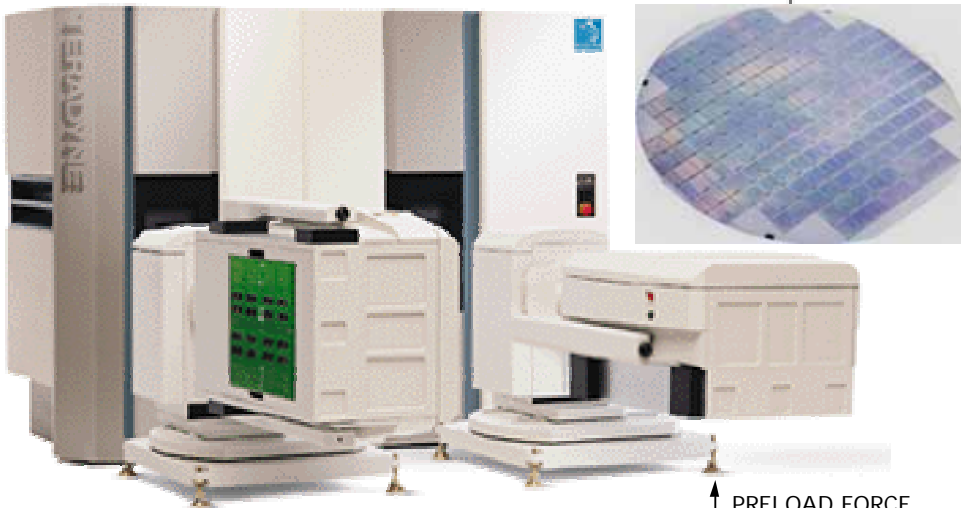


<i>Engine QKC</i>	<u>8 dowels</u>	<u>QKC</u>
Precision pieces	8	3
Precision features	16	6
Tolerance [microns]	40	80
Repeatability [microns]	5	1.5
Cost reduction/engine	N/A	\$1

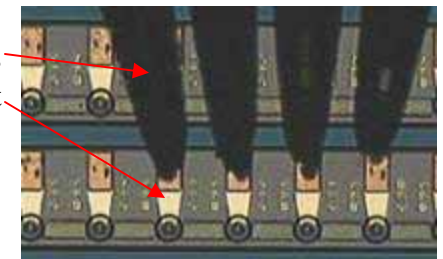
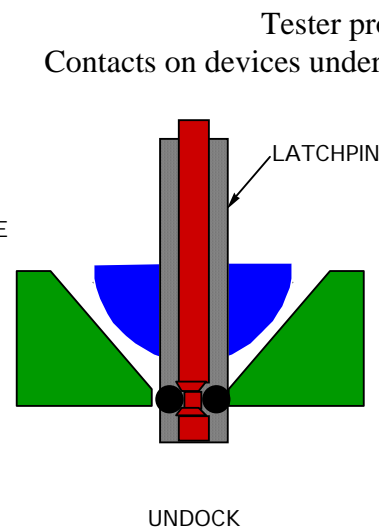
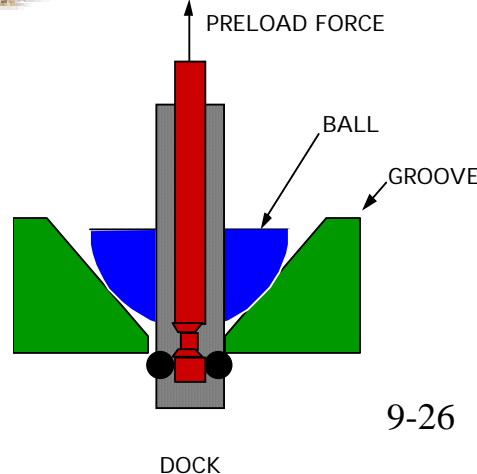
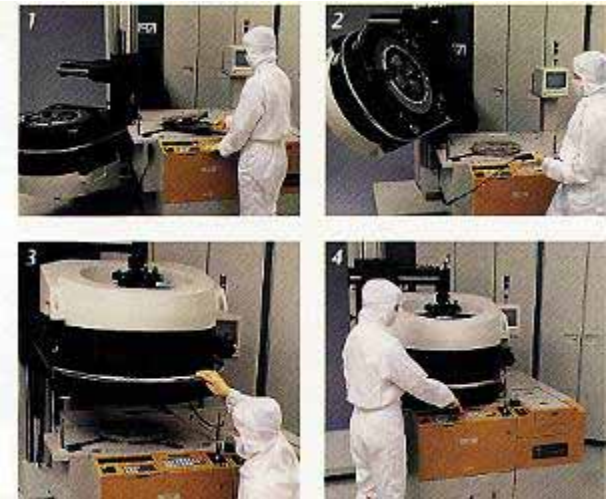


Kinematic Couplings: *Servo-Controlled*

- Automatic Test Equipment (ATE) is used to test computer chips during their manufacture
 - Testing wafers requires a very high precision interface between the tester and wafer
- Servo-controlled kinematic couplings automatically level ATE test heads to wafer plane
 - Michael Chiu's Doctoral Thesis (US Patent #5,821,764, Oct. 1998)
- Teradyne has shipped over 500 systems

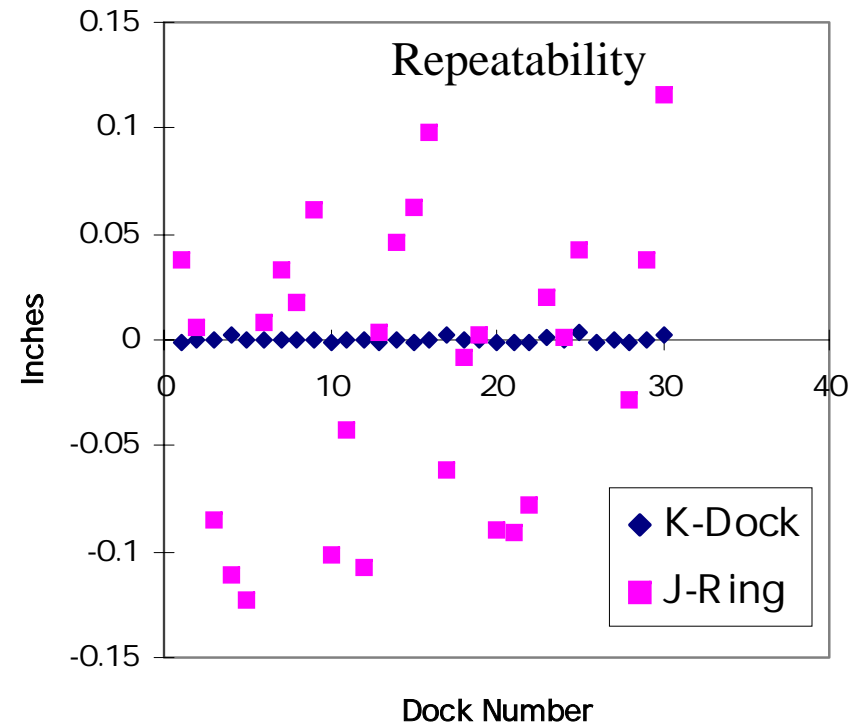
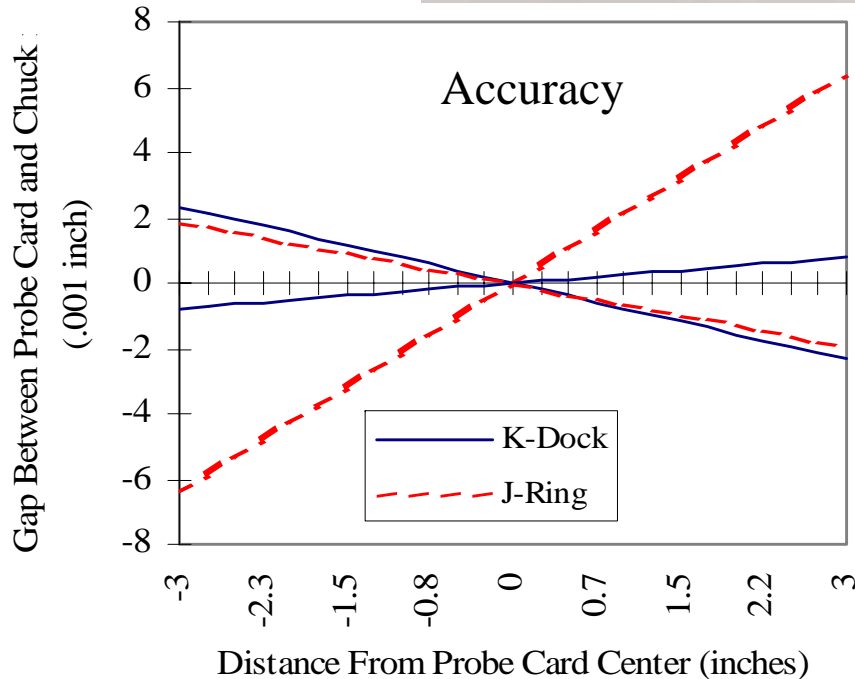
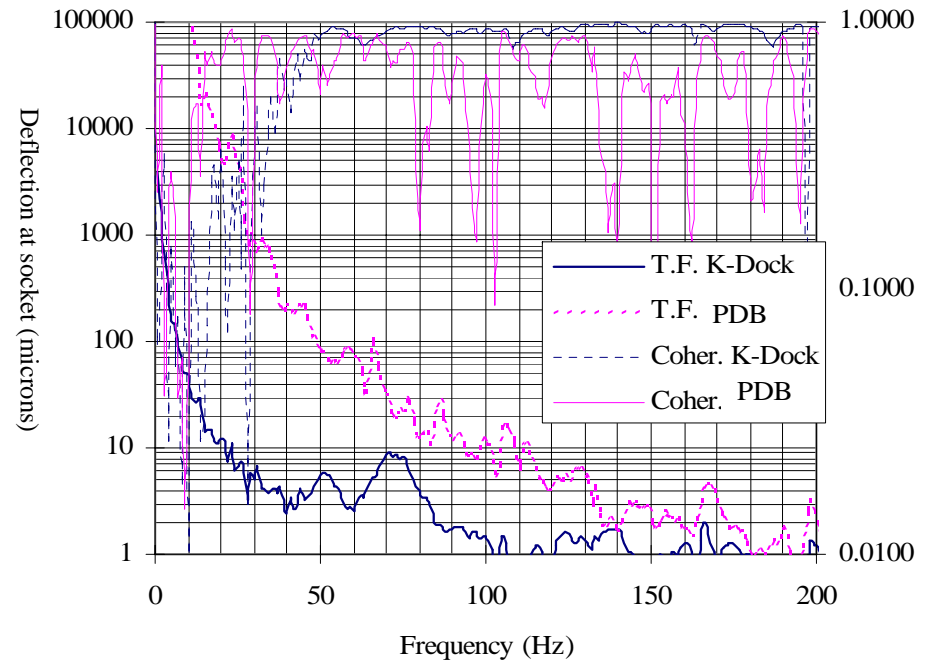
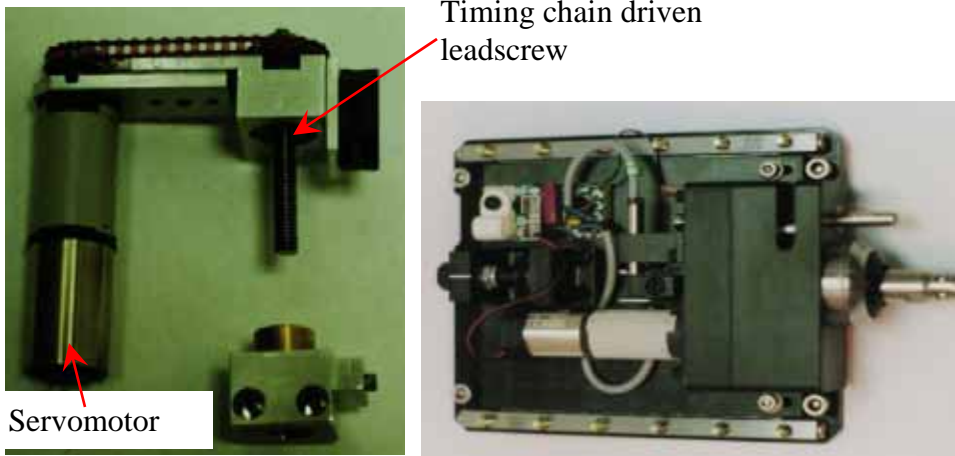


- 1 The operator inserts a probe cord into the J971's probe interface.
- 2 The test station is electrically guided into probe position.
- 3 Alignment pins dock the test station on the probe.
- 4 The test station is locked into position, ready to test wafers.



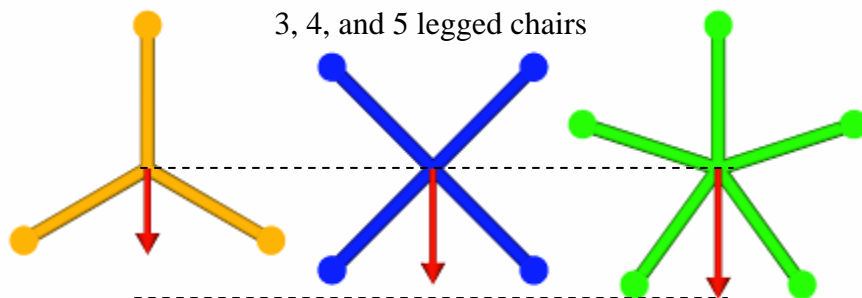
SCKC: *Details*

- Improved repeatability, accuracy, dynamic stiffness

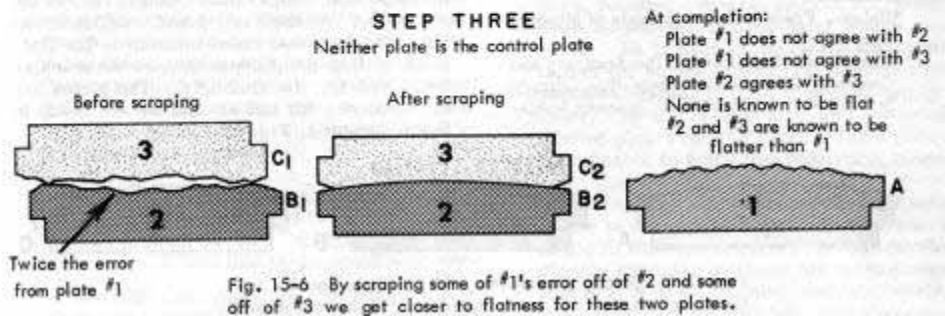
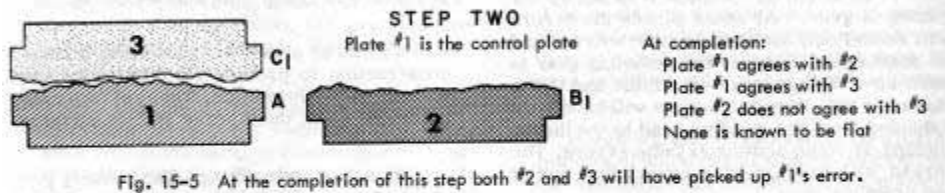
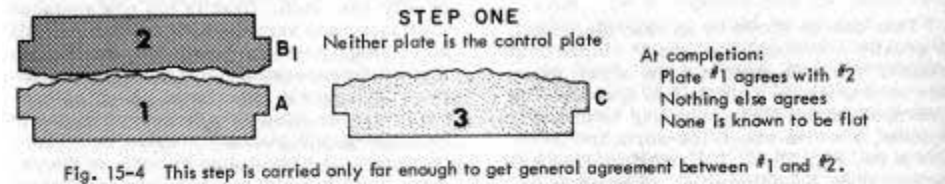


Elastic Averaging

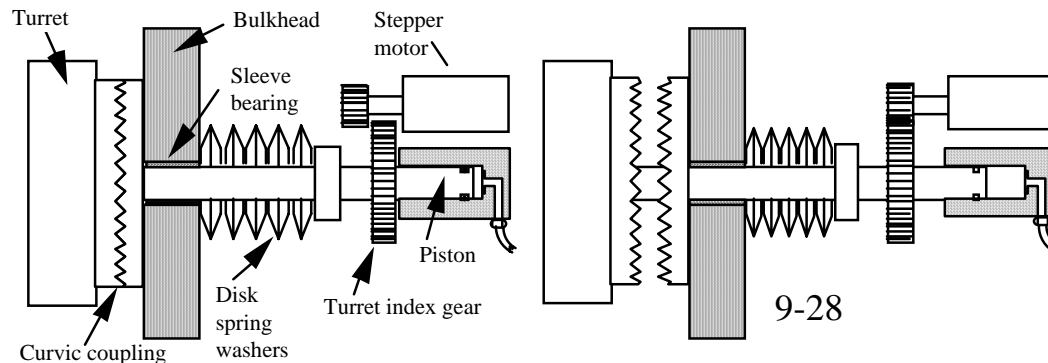
- Any one error can be averaged out by having many similar features
 - As in gathering data with random errors, the accuracy of the reading is proportional to the square root of the number of samples taken
- Local errors are accommodated by elastically deforming the members
 - Overall high stiffness is obtained by the sum of many compliant members



Scraping plates flat, the genesis of all precision machines



From T. Busch, *Fundamentals of Dimensional Metrology*, Delmar Publishers, Albany, NY, 1964



Curvic coupling mechanism for indexing precision machine tools

Elastic Averaging: *Overconstraint?*

- Over-constraint is NOT Elastic Averaging
 - Example: One component (a carriage) wants to move along one path and another (ballscrew nut) along another, but they are attached to each other
 - They will resist each other, and high forces can result which accelerates wear
 - Either more accurate components and assembly are required, or compliance, or clearance (pin in oversized hole) must be provided between the parts
 - Designers should always be thinking of not just an instant along motion path, but along the entire motion path



The coupling may be elastic, but to get it to bend, means large forces are placed on the delicate motor shaft!

