Architectural geometry: Boolean Operations

2009년 1월 22일 발표자: 유중현

Typical modeling functions



- Creation by simple shapes
 - primitive creation function and Boolean operation
- Creation by moving surfaces
 - sweeping, skinning
- Modification of existing shapes
 - rounding (blending), lifting, filleting etc.
- Manipulation of the low level entities of a solid, such as vertices, edges and faces
 - boundary modeling
- Modeling by using familiar shapes
 - feature-based modeling



Primitive creation function

Retrieve a solid from the х primitive solids stored in CAD system. D Cylinder Block y User specifies the х R parameters for primitives. Sphere Cone R_2 Η R_1 R_0 'n x Torus Wedge

Boolean operations

- Tools for modeling solid by combining the primitives or existing shapes.
- Union, intersection and difference
 - Trimming + joining
 - Split
 - Be careful that invalid solids should not appear.





Sweeping



- Translational sweeping
- Rotational sweeping (Swinging)



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- Trajectory
- Cross-section
- (Lofting)

Skinning



Rounding



Rounding (Blending)Filleting









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Lifting



- Extrusion
- Protrusion (Boss)



Boundary modeling



Tweaking



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Feature-based modeling



- Feature = geometric information + functional information (design history)
 - Body feature, form feature, operation feature
 - Ex) hole = positioning of cylinder + Boolean difference



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Parametric modeling



- Modeling based on geometric constraint and dimension data
 - Constraint
 - Two edges lie in a plane.
 - Two faces are parallel.
 - Dimension
 - Relationship among dimensions as well



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Architectural geometry: Planar transformations

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2D transformation



- Affine transformation
 - Congruent transformation: preserve length and angle
 - Translation, rotation, reflection
 - (Isometries)
 - Similarity transformation: preserve angle
 - Shear transformation: preserve area

ν̈́

 $ightarrow T(\vec{v}_1) = \vec{v}_1$ $\mathbf{r} \vec{v}_1$ $\rightarrow \vec{v}_1$ O = T(O) $x_1 = x + y \tan \theta$ fixed line: x-axis $y_1 = y$ x_1 = xfixed line: y-axis $y_1 = x \tan \theta + y$

θ

Shearing

 \vec{v}_2



 $\pi/2 - \theta$

 $T(\vec{v}_2)$

Composition of transformations



- Composition of two reflections
 - Intersecting reflection lines: a rotation
 - Parallel reflection lines: a translation
- Composition of two opposite or two direct congruence transformation
 - A direct congruence transformation
- Composition of a direct and an opposite congruence transformation
 - An opposite congruence transformation

Tilings



- Regular and semi-regular tessellation (tiling)
 - Regular: triangle, square and hexagon
 - Semi-regular: eight tessellation in a plane (3, 3, 4, 4) ...

Crystallographic groups

- The groups of congruence transformations which make a tiling invariant under the transformations
- 17 groups (28 different types of tiles)