#### Logic and Computer Design Fundamentals

## Chapter 3 – Combinational Logic Design

Part 1 – Implementation Technology and Logic Design

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## **Overview**

- Part 1 Design Procedure
  - Steps
    - Specification
    - Formulation
    - Optimization
    - Technology Mapping
  - Beginning Hierarchical Design
  - Technology Mapping AND, OR, and NOT to NAND or NOR
  - Verification
    - Manual
    - Simulation

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## **Overview** (continued)

#### Part 2 – Combinational Logic

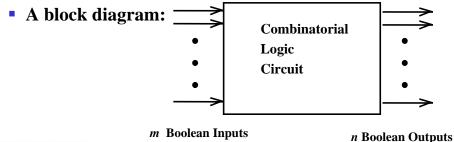
- Functions and functional blocks
- Rudimentary logic functions
- Decoding using Decoders
  - Implementing Combinational Functions with Decoders
- Encoding using Encoders
- Selecting using Multiplexers
  - Implementing Combinational Functions with Multiplexers

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#### **Combinational Circuits**

- A combinational logic circuit has:
  - A set of *m* Boolean inputs,
  - A set of *n* Boolean outputs, and
  - *n* switching functions, each mapping the 2<sup>m</sup> input combinations to an output such that the current output depends only on the current input values



### **Design Procedure**

- 1. Specification
  - Write a specification for the circuit if one is not already available
- 2. Formulation
  - Derive a truth table or initial Boolean equations that define the required relationships between the inputs and outputs, if not in the specification
  - Apply hierarchical design if appropriate
- 3. Optimization
  - Apply 2-level and multiple-level optimization
  - Draw a logic diagram or provide a netlist for the resulting circuit using ANDs, ORs, and inverters

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## **Design Procedure**

- 4. Technology Mapping
  - Map the logic diagram or netlist to the implementation technology selected
- 5. Verification
  - Verify the correctness of the final design manually or using simulation

#### **Design Example**

- **1.** Specification
  - BCD to Excess-3 code converter
  - Transforms BCD code for the decimal digits to Excess-3 code for the decimal digits
  - BCD code words for digits 0 through 9: 4-bit patterns 0000 to 1001, respectively
  - Excess-3 code words for digits 0 through 9: 4bit patterns consisting of 3 (binary 0011) added to each BCD code word
  - Implementation:
    - multiple-level circuit
    - NAND gates (including inverters)

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## Design Example (continued)

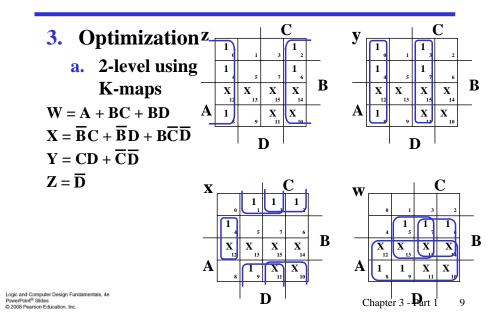
#### 2. Formulation

• Conversion of 4-bit codes can be most easily formulated by a truth table

•	Variables	Input BCD	Output Excess-3
	- <u>BCD</u> :	<b>ABCD</b>	WXYZ
	A,B,C,D	0000	0011
•	Variables	0001	0100
	- Excess-3	0010	0101
		0011	0110
•	W,X,Y,Z	0100	0111
	Don't Cares	0101	1000
	- BCD 1010	$\begin{array}{c} 0 \ 1 \ 1 \ 0 \\ 0 \ 1 \ 1 \ 1 \end{array}$	1001 1010
	to 1111		
		1000	1011
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### **Design Example** (continued)



### **Design Example** (continued)

- **3.** Optimization (continued)
  - b. Multiple-level using transformations W = A + BC + BD  $X = \overline{B}C + \overline{B}D + B\overline{C}\overline{D}$   $Y = CD + \overline{C}\overline{D}$   $Z = \overline{D}$  G = 7 + 10 + 6 + 0 = 23
  - Perform extraction, finding factor:

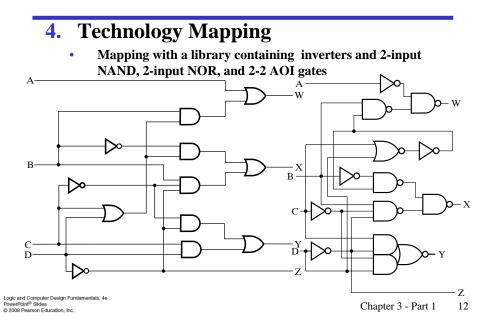
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### **Design Example** (continued)

#### **3.** Optimization (continued)

b. Multiple-level using transformations  $\mathbf{T}_1 = \mathbf{C} + \mathbf{D}$  $W = A + BT_1$  $\mathbf{X} = \overline{\mathbf{B}}\mathbf{T}_1 + \mathbf{B}\overline{\mathbf{C}}\overline{\mathbf{D}}$  $\mathbf{Y} = \mathbf{C}\mathbf{D} + \overline{\mathbf{C}}\overline{\mathbf{D}}$  $\mathbf{Z} = \overline{\mathbf{D}}$ G = 19 An additional extraction not shown in the text since it • uses a <u>Boolean transformation</u>:  $(\overline{C}\overline{D} = \overline{C} + \overline{D} = \overline{T}_1)$ :  $W = A + BT_1$  $\mathbf{X} = \overline{\mathbf{B}} \mathbf{T}_1 + \mathbf{B} \overline{\mathbf{T}}_1$  $\mathbf{Y} = \mathbf{C}\mathbf{D} + \overline{\mathbf{T}}_1$  $\mathbf{Z} = \overline{\mathbf{D}}$ G = 2 + 1 + 4 + 6 + 4 + 0 = 16!Logic and Computer Design Funda PowerPoint<sup>®</sup> Slides © 2008 Pearson Education, Inc. Chapter 3 - Part 1 11

### **Design Example** (continued)



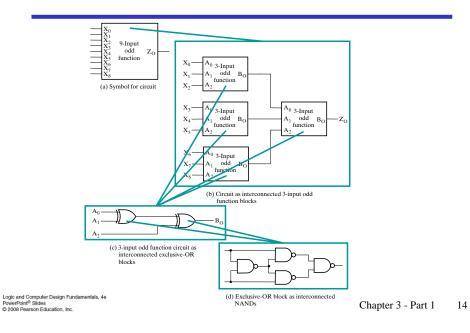
## **Beginning Hierarchical Design**

- To control the complexity of the function mapping inputs to outputs:
  - Decompose the function into smaller pieces called *blocks*
  - Decompose each block's function into smaller blocks, repeating as necessary until all blocks are small enough
  - Any block not decomposed is called a primitive block
  - The collection of all blocks including the decomposed ones is a *hierarchy*
- Example: 9-input parity tree (see next slide)
  - Top Level: 9 inputs, one output
  - 2nd Level: Four 3-bit odd parity trees in two levels
  - 3rd Level: Two 2-bit exclusive-OR functions
  - Primitives: Four 2-input NAND gates
  - Design requires 4 X 2 X 4 = 32 2-input NAND gates

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### **Hierarchy for Parity Tree Example**



### **Reusable Functions**

- Whenever possible, we try to decompose a complex design into common, *reusable* function blocks
- These blocks are
  - verified and well-documented
  - placed in libraries for future use

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## **Top-Down versus Bottom-Up**

- A *top-down design* proceeds from an abstract, highlevel specification to a more and more detailed design by decomposition and successive refinement
- A *bottom-up design* starts with detailed primitive blocks and combines them into larger and more complex functional blocks
- Design usually proceeds top-down to known building blocks ranging from complete CPUs to primitive logic gates or electronic components.
- Much of the material in this chapter is devoted to learning about combinational blocks used in top-down design.

## **Technology Mapping**

- Mapping Procedures
  - To NAND gates
  - To NOR gates
  - Mapping to multiple types of logic blocks in covered in the reading supplement: Advanced Technology Mapping.

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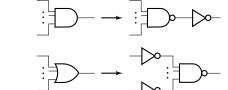
## Mapping to NAND gates

- Assumptions:
  - · Gate loading and delay are ignored
  - Cell library contains an inverter and *n*-input NAND gates, *n* = 2, 3, ...
  - An AND, OR, inverter schematic for the circuit is available
- The mapping is accomplished by:
  - Replacing AND and OR symbols,
  - Pushing inverters through circuit fan-out points, and
  - Canceling inverter pairs

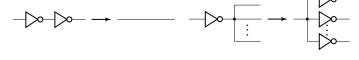
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### **NAND Mapping Algorithm**

**1.** Replace ANDs and ORs:



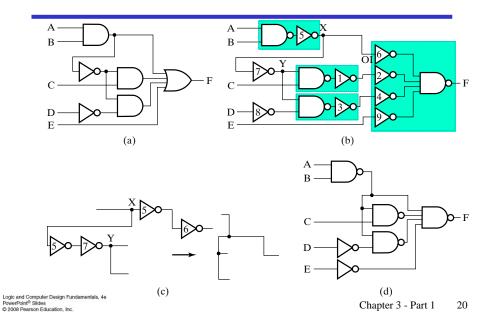
- 2. Repeat the following pair of actions until there is at most one inverter between :
  - a. A circuit input or driving NAND gate output, and
  - **b.** The attached NAND gate inputs.



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## **NAND Mapping Example**



## Mapping to NOR gates

#### • Assumptions:

- · Gate loading and delay are ignored
- Cell library contains an inverter and *n*-input NOR gates, *n* = 2, 3, ...
- An AND, OR, inverter schematic for the circuit is available

#### The mapping is accomplished by:

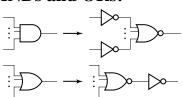
- Replacing AND and OR symbols,
- Pushing inverters through circuit fan-out points, and
- Canceling inverter pairs

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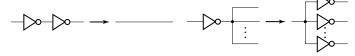
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## **NOR Mapping Algorithm**

**1.** Replace ANDs and ORs:

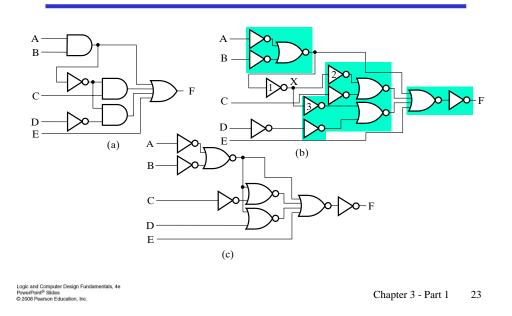


- 2. Repeat the following pair of actions until there is at most one inverter between :
  - a. A circuit input or driving NAND gate output, and
  - **b.** The attached NAND gate inputs.



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## **NOR Mapping Example**



## Verification

- Verification show that the final circuit designed implements the original specification
- Simple specifications are:
  - truth tables
  - Boolean equations
  - HDL code
- If the above result from <u>formulation</u> and are not the <u>original specification</u>, it is critical that the formulation process be flawless for the verification to be valid!

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### **Basic Verification Methods**

- Manual Logic Analysis
  - Find the truth table or Boolean equations for the final circuit
  - Compare the final circuit truth table with the specified truth table, or
  - Show that the Boolean equations for the final circuit are equal to the specified Boolean equations
- Simulation
  - Simulate the final circuit (or its netlist, possibly written as an HDL) and the specified truth table, equations, or HDL description using test input values that fully validate correctness.
  - The obvious test for a combinational circuit is application of all possible "care" input combinations from the specification

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#### **Verification Example: Manual Analysis**

- BCD-to-Excess 3 Code Converter
  - Find the SOP Boolean equations from the final circuit.
  - Find the truth table from these equations
  - Compare to the formulation truth table
- Finding the Boolean Equations:  $T_1 = \overline{\overline{C} + \overline{D}} = C + D$   $W = \overline{\overline{A}} (\overline{T_1 B}) = A + B T_1$   $X = (T_1 B) (B \overline{C} \overline{D}) = \overline{B} T_1 + B \overline{C} \overline{D}$  $Y = \overline{C\overline{D} + \overline{C}D} = CD + \overline{C}\overline{D}$

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#### **Verification Example: Manual Analysis**

Find the circuit truth table from the equations and compare

to specification truth table:			
Input BCD	Output Excess-3		
A B C D	WXYZ		
0000	0011		
0001	0100		
0010	0101		
0011	0110		
0100	0111		
0101	1000		
0110	1001		
0111	1010		
1000	1011		
1001	1011		

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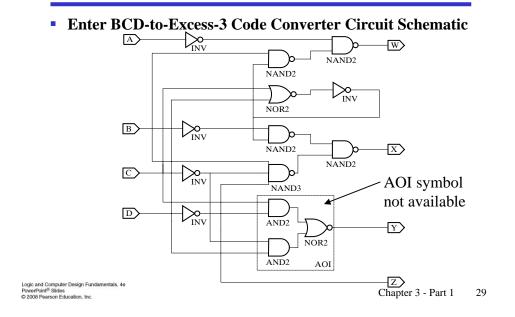
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# Verification Example: Simulation

#### Simulation procedure:

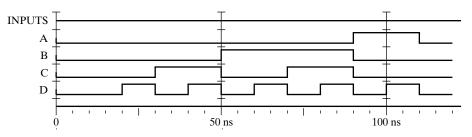
- Use a schematic editor or text editor to enter a gate level representation of the final circuit
- Use a waveform editor or text editor to enter a test consisting of a sequence of input combinations to be applied to the circuit
  - This test should guarantee the correctness of the circuit if the simulated responses to it are correct
  - Short of applying all possible "care" input combinations, generation of such a test can be difficult

#### **Verification Example: Simulation**



#### **Verification Example: Simulation**

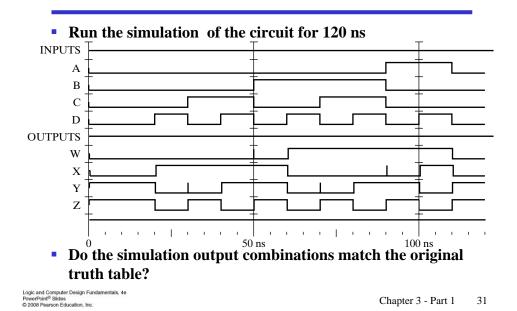
Enter waveform that applies all possible input combinations:



 Are all BCD input combinations present? (Low is a 0 and high is a one)

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#### **Verification Example: Simulation**



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